

# The Voting Premium\*

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## Abstract

This paper develops a unified theory of blockholder governance and the voting premium. It explains how a voting premium emerges when a minority blockholder tries to influence the composition of the shareholder base, in a setting without takeovers and controlling shareholders. The model shows that empirical measures of the voting premium generally do not reflect the value of voting rights, and that the voting premium can be negligible even when the allocation of voting rights is important. Moreover, the model can explain a negative voting premium, which has been documented in several studies. It arises because of free-riding by dispersed shareholders on the blockholder's trades, which increases the price impact of trading voting shares and makes them less liquid than non-voting shares. The model also has novel implications for the relationship between the voting premium and the severity of conflicts of interest between shareholders, the price of a separately traded vote, and competition for control among blockholders.

**Keywords:** Voting, trading, voting premium, blockholders, ownership structure, shareholder rights, corporate governance

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# 1 Introduction

Voting is a central mechanism of corporate governance. It empowers shareholders of publicly traded companies to elect directors, approve major corporate transactions, and decide on governance, social, and environmental policies. Most corporations have blockholders who are large enough to influence voting outcomes (La Porta et al. (1999); McCahery, Sautner, and Starks (2016); Edmans and Holderness (2017); Dasgupta, Fos, and Sautner (2020)). Blockholders' desire to accumulate voting power and exert corporate influence can affect stock prices and give rise to a voting premium.

The asset pricing implications of control rights have been studied extensively. The theoretical literature followed Grossman and Hart (1988) and Harris and Raviv (1988), and attributed the voting premium almost exclusively to control contests and takeovers. This is puzzling in light of a large empirical literature in this area. First, the most common measure of the voting premium is arguably the dual-class premium, which appears to be largest in economies in which control contests are rare, and which does not disappear when regulation requires equal treatment of non-voting shares in takeovers.<sup>1</sup> Second, while all studies find the voting premium to be positive on *average*, many studies document negative voting premiums for some firms, which is difficult to explain in a model with bidding contests. Third, studies that construct non-voting shares synthetically to estimate the voting premium find that it is largest around shareholder meetings compared to other periods of the year (e.g., Kalay, Karakas, and Pant (2014)), which highlights the importance of voting on proposals for the existence of a voting premium. Last, recent studies estimate the voting premium from fees in equity lending markets or price changes around record dates. They usually find negligible values for voting rights, which is in conflict with the earlier literature and adds another puzzle.

Overall, these gaps and conflicting conclusions suggest that the theoretical underpinnings of the voting premium are still incomplete. To address these challenges, this paper develops a unified theory of blockholder governance and the voting premium. We study how and why a voting premium emerges in the absence of takeovers or controlling shareholders, which is arguably the empirically most relevant setting.

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<sup>1</sup>See our extensive discussion of the empirical literature in Section 8 and in the Appendix, which shows large dual-class premiums for France, Israel, and Italy, among others, whereas the lowest dual-class premiums are found in the US.

We analyze a model with a continuum of atomistic dispersed shareholders and one minority blockholder. The baseline model features one-share-one-vote. Shareholders first trade with each other in a competitive stock market. Those who own shares after trading then vote on a proposal at a shareholder meeting. Shareholders observe a public signal about the quality of the proposal before they cast a vote, and the proposal is approved if enough votes are cast in favor. Shareholders differ in their preferences for the proposal: While some shareholders are skeptical and need a lot of evidence to vote in favor, others are more disposed toward the proposal and generally support it. Such heterogeneity may arise from differences in investment horizons; tax status; ownership of other firms; attitudes toward risk, corporate governance philosophies, and social and political ideologies.<sup>2</sup>

In our framework, the voting outcomes, the composition of the shareholder base, and asset prices are all endogenous. In equilibrium, the proposal is approved if and only if the public signal about its quality exceeds a certain cutoff. Shareholders are heterogeneous, so the proposal is accepted too often from the point of view of some, and rejected too often from the perspective of others. We call the shareholder who fully agrees with the decision rule implied by the cutoff the “median voter;” the median voter’s identity completely characterizes the expected voting outcome. Importantly, the median voter can be either a dispersed shareholder or a blockholder, and his identity is determined by the composition of the shareholder base after trading. Hereafter, the term “median voter” is used interchangeably with the expected voting outcome.

The blockholder and dispersed shareholders trade in anticipation of the expected voting outcome and its impact on their valuations; shareholders’ valuations could differ because of heterogeneous preferences. Trading reallocates cash flow rights and voting rights across shareholders, since shares are bundles of both. Price-taking dispersed shareholders trade only for cash flow reasons, i.e., if the share price differs from their private valuations. By contrast, the blockholder can be pivotal for the voting outcome, so he may also purchase shares to influence the voting outcome, that is, to push the median voter in his preferred direction.

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<sup>2</sup>See the following literature on each of these issues: Investor time horizons: [Bushee \(1998\)](#) and [Gaspar, Massa, and Matos \(2005\)](#); tax status: [Desai and Jin \(2011\)](#); conflicts of interest and common ownership: [Cvijanovic, Dasgupta, and Zachariadis \(2016\)](#) and [He, Huang, and Zhao \(2019\)](#); attitudes to corporate governance and social and political ideologies: [Bolton et al. \(2020\)](#) and [Bubb and Catan \(2021\)](#). [Hayden and Bodie \(2008\)](#) provide a comprehensive overview of different sources of shareholder heterogeneity.

The equilibrium share price can be decomposed into two terms. The first term captures the market clearing price in the hypothetical scenario in which all shareholders anticipate exactly the same decision rule as the one that actually arises, but take it as exogenously given. This price would emerge if trading of shares did not reallocate voting rights across shareholders, e.g., if trade happened after the record date or if shares did not contain voting rights. The second term is the additional component in the stock price that arises exactly because the trading of shares reallocates the voting rights across shareholders, moves the median voter, and thereby changes the value of the shares for small shareholders. We call this term the *voting premium* and show that it reflects the blockholder's equilibrium net marginal payoff from buying one additional voting right.

Our theoretical definition of the voting premium has two appealing empirical counterparts. First, our definition of the voting premium captures the dual-class premium: In an extension to a dual-class setting, the price differential between voting and non-voting shares reflects the blockholder's net marginal payoff from buying an additional voting right. Second, the voting premium can be considered as the difference between the pre-record date and the post-record date share price. The expected voting outcome is the same at both moments in time, but after the record date, trading no longer reallocates voting rights for decisions taken at the upcoming meeting. However, our definition of the voting premium is more general and extends to single-class firms and to dates other than the record date.

We show that a positive voting premium can arise in equilibrium even though there are no takeovers in our model and the blockholder does not obtain a controlling stake. Intuitively, as the blockholder buys more shares, he moves the median voter, who becomes more similar to the blockholder. If the blockholder accumulates enough shares, he even becomes the median voter himself. However, since voting rights are not traded separately from cash flow rights, this accumulation of voting power requires dispersed shareholders who like the expected voting outcome to sell more of their shares. Their heterogeneous valuations create an upward-sloping supply function to the blockholder, which results in price impact.

The voting premium equals the blockholder's benefit of purchasing one additional voting right, net of the price impact of this additional purchase on his entire trade. If his price impact is significant, the blockholder optimally limits his accumulation of shares and, hence, his voting power; then the voting premium is positive. Conversely, if price impact is moderate,

the blockholder will buy sufficiently many shares to become the median voter. Then, any further purchases would leave the voting outcome unchanged and the voting premium is zero. Therefore, our model can explain empirical studies that document a negligible voting premium (e.g., [Christoffersen et al. \(2007\)](#) and [Fos and Holderness \(2020\)](#)).

The case of a zero voting premium illustrates the general principle that the voting premium does not reflect the economic value of voting rights, because it captures only the blockholder's *marginal* value from an additional vote, net of his price impact and evaluated at his optimal ownership level. However, the blockholder's total value of voting rights reflects his average willingness to buy votes, which includes all the infra-marginal trades from his initial endowment to his equilibrium ownership. In this respect, the voting premium underestimates the importance of voting rights. This observation is important for interpreting empirical findings, since some proxies for the voting premium measure the marginal value of a vote (dual-class share premium; price drop on record days), whereas others are more related to the average value of voting rights (block premium).

For the same reasons, the voting premium is not a good measure of voting power. Voting power is related to the blockholder's likelihood of being pivotal and swinging the voting outcome. However, an increase in the blockholder's voting power decreases his distance from the median voter, and thus his valuation of a marginal vote. Therefore, the magnitude of the voting premium is generally unrelated to the blockholder's voting power, and this relationship can even be negative when the blockholder becomes the median voter himself: Then his voting power is large and the voting premium is zero. Thus, the voting premium emerges not from the blockholder's accumulation of voting power, but from his indirect influence on the voting outcome through the composition of the shareholder base.

Our model can also rationalize a negative voting premium, which has been documented in several studies. A negative voting premium implies that the blockholder limits his purchases of voting shares in order to commit to a reduced influence on the voting outcome. Such a strategy may appear puzzling because the benefit of a marginal vote to the blockholder is always positive, since the value of his endowment always increases if he moves the median voter toward himself. However, if the blockholder has a small endowment, his main focus is on his trading profits, which can become negative if his price impact is sufficiently large. Consequently, the blockholder buys fewer shares compared to a scenario in which shares do not have voting

rights, and the voting premium becomes negative. To see how this can happen, consider a scenario in which the blockholder favors acceptance of a certain proposal, e.g., adoption of an environmentally friendly production technology, but dispersed shareholders are on average more environmentalist and value this voting outcome even more than the blockholder himself. This increases the price at which they supply shares: they free ride on the blockholder's trades. Then the blockholder's price impact can be so large that further purchases would increase the stock price even more than his own valuation, giving rise to a negative voting premium.

The discussion above reflects the more general insight that the voting rights embedded in the shares can either amplify or attenuate the price impact of trades. If the blockholder's trades move the median voter in the direction preferred by dispersed shareholders, they increase the price at which they supply their shares to the blockholder. Then his price impact is amplified compared to a scenario in which shares do not have voting rights. However, if the blockholder is in conflict with dispersed shareholders, then his trades push the median voter away from their desired point and thus reduce the price at which they are willing to sell, attenuating price impact. Overall, this argument implies that liquidity, if measured by price impact, is endogenous in our setting and generally differs between voting and non-voting shares. Thus, we can also view the negative voting premium through the lens of endogenous liquidity, and our explanation for the negative voting premium is broadly consistent with the empirical literature. This literature sometimes attributes the negative voting premium to the lower liquidity of superior voting shares.<sup>3</sup> However, the differential liquidity of voting and non-voting shares in our model arises endogenously from the impact of the blockholder's trades on dispersed shareholders' valuations.

The literature often associates the voting premium with conflicts of interest and sometimes uses it as a measure for private benefits of control. Hence, we investigate how the voting premium depends on the divergence between the preferences of the blockholder and dispersed shareholders. This relationship is nuanced. In some cases, a higher voting premium is associated with a higher payoff for the blockholder and lower payoffs for small shareholders, in line with the argument that the voting premium indicates a conflict of interest. However, in other

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<sup>3</sup>? and Gardiol, Gibson-Asner, and Tuchschnid (1997) are probably the first to show how liquidity differences between classes of stock differentiated by ownership and voting restrictions lead to a price premium. Neumann (2003), Odegaard (2007), and Broussard and Vaihekoski (2019) explain their observations of a negative voting premium with liquidity differences between voting and non-voting shares.

cases, the voting premium is higher when both, the blockholder's and the small shareholders' payoffs are higher. This happens if the preferences of small shareholders are skewed, or with a supermajority requirement; in both cases the average small shareholder differs from the median voter. Hence, the voting premium is not necessarily positively associated with the severity of conflicts between different shareholders, and, therefore, is probably also not a good measure for them.

We extend the model in a number of ways to explore additional questions. First, we consider a setting in which voting rights are traded separately, e.g., through share lending, and show that the price of a separately traded vote can be zero even if the voting premium for a share in which voting and cash flow rights are bundled is strictly positive. Second, we introduce multiple blockholders to analyze how the competition among them and their heterogeneous preferences affect the voting premium. Last, we consider a setting in which decisions are made not by voting, but by managers who consider the preferences of the entire shareholder base. We show that the blockholder's trades can then give rise to an "influence premium" in the share price, which is different from the voting premium and can even be larger.

After concluding our theoretical analysis, in Section 8 we use our insights to shed some light on the large number of empirical studies on the voting premium. We distinguish five different methodologies that have been used to measure the voting premium and argue that the large differences of estimates across methodologies are unsurprising. We also discuss findings on the time-series variation and cross-sectional variation of the voting premium in light of our model.

Overall, our paper makes three contributions. First, it examines the trading between small and large shareholders and the ownership structure of the firm in a context in which blockholders affect voting outcomes without majority control. Second, it contributes to our understanding of asset prices by showing how and when a voting premium emerges when blockholders can acquire voting control only through securities in which cash flow rights are bundled with voting rights. Third, it provides guidance to the empirical literature by showing how different proxies for the voting premium are related and why they may be different from each other.

## 2 Discussion of the literature

We contribute a new theory of the value of voting rights. The primary approach in the literature, pioneered by [Grossman and Hart \(1988\)](#) and [Harris and Raviv \(1988\)](#), considers settings with control contests of firms with dual-class shares. In this approach, rival bidders and incumbent managers differ in their ability to generate cash flows that are shared by all shareholders, and in their valuation of private benefits from controlling the firm. Bidders compete for control and pay a premium to the holders of the voting shares.<sup>4</sup> Studies in this literature have explored a range of alternative settings, including different types of admissible bids; variation in the ability to extract private benefits; settings without a free-rider problem; and frictions from asymmetric information.<sup>5</sup> Moreover, some studies have considered deviations from the one-share one-vote principle through trading in derivatives rather than in non-voting shares (e.g., [Blair, Golbe, and Gerard \(1989\)](#); [Kalay and Pant \(2010\)](#); [Burkart and Lee \(2010\)](#); [Dekel and Wolinsky \(2012\)](#)). Independently of the details, a wide range of settings give rise to a voting premium in a bidding contest. Our theory contributes to this literature by showing how a voting premium emerges without takeovers and control contests. The critical point of departure is the way in which the blockholder’s (respectively, bidder’s) higher willingness to pay translates into a higher stock price. In control contests, this happens because competition among bidders or the free-rider problem force bidders to pay a higher price (see [Bergström and Rydqvist \(1992\)](#)) and [Zingales \(1995\)](#) for similar observations). However, neither mechanism is present in our model, which does not feature majority control. Instead, in our setting, the blockholder’s trades affect the reservation prices of small shareholders, which generates an upward-sloping supply curve to the blockholder.<sup>6</sup> This may give rise to a positive voting premium even if the blockholder does not acquire majority control, and a negative voting premium may result if this supply curve becomes sufficiently steep.

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<sup>4</sup>[Burkart and Lee \(2008\)](#) survey theoretical work on the role of the security-voting structure and the control premium in the context of takeovers.

<sup>5</sup>Types of admissible bids: [Vinaimont and Sercu \(2003\)](#); [Dekel and Wolinsky \(2012\)](#); variation in whether one party has private benefits: none: [Bergström and Rydqvist \(1992\)](#); one party is the main case in [Grossman and Hart \(1988\)](#); both parties: [Vinaimont and Sercu \(2003\)](#); [Burkart, Gromb, and Panunzi \(1998\)](#); there is no free-rider problem in [Bergström and Rydqvist \(1992\)](#); asymmetric information: [Burkart and Lee \(2010\)](#). Some empirical contributions also include further modeling efforts to motivate specific empirical analyses, e.g., [Zingales \(1995\)](#); [Rydqvist \(1996\)](#).

<sup>6</sup>An upward-sloping supply curve is also present in takeover models with majority control of [Stulz \(1988\)](#) and [Burkart, Gromb, and Panunzi \(1998\)](#). The latter also introduce the term “upward-sloping supply function.”



A complementary literature analyzes a market in which votes trade separately from shares.<sup>7</sup> While these papers differ significantly regarding their chosen settings and normative conclusions, they all conclude that the value of separately traded votes is negligible, either because dispersed shareholders value votes in proportion to their probability of being pivotal (Neeman and Orosel (2006); Brav and Mathews (2011); Speit and Voss (2020)) or because uninformed shareholders would like their votes to be picked up and cast by informed shareholders (Esö, Hansen, and White (2014)).<sup>8</sup> As our analysis emphasizes, the price of a vote traded separately can be very different from the price of a vote that is traded in conjunction with cash flow rights. In particular, in our extension to a separate market for votes, the voting premium for shares that combine cash flow and voting rights can be strictly positive even though the price of separately traded votes is zero.

The only approach that has derived a significant voting premium without control contests is Rydqvist (1987), who builds on Milnor and Shapley (1978) and introduces the notion of an oceanic Shapley value to the analysis of dual-class shares. The critical step here is that the ocean of atomistic shareholders can *collectively* become pivotal and thus value their voting power. However, this leaves open how these atomistic shareholders resolve their collective action problem. In our setting, each dispersed shareholder maximizes only his individual payoff.

Our paper also contributes to the literature on the equilibrium ownership structure of firms and the analysis of blockholders. A large strand of this literature is on direct intervention by blockholders (“voice”).<sup>9</sup> Another strand of this literature analyzes how trading by blockholders affects governance through its impact on stock prices and managers’ incentives (“exit”).<sup>10</sup> By contrast, in our setting, the blockholder exercises influence by affecting the identity of the median voter. This is empirically important because many blockholders, notably financial

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<sup>7</sup>It is largely motivated by concerns about the incentives created by decoupling votes from cash flow rights (“empty voting”), triggered by a sequence of papers by Hu and Black, e.g., Hu and Black (2007); Hu and Black (2015).

<sup>8</sup>These papers focus on vote trading in corporations. A related literature in political science examines how vote trading allows agents with a higher intensity of preferences to buy votes from those who care about the decision less. See, e.g., Casella, Llorente-Saguer, and Palfrey (2012) and the literature surveyed in that paper.

<sup>9</sup>See Admati, Pfleiderer, and Zechner (1994), Bolton and von Thadden (1998), Kahn and Winton (1998), and Maug (1998) for earlier contributions to this literature. See the surveys of Edmans (2014), Edmans and Holderness (2017), and Dasgupta, Fos, and Sautner (2020) for more recent work and further details.

<sup>10</sup>See Admati and Pfleiderer (2009), Edmans (2009), Edmans and Manso (2011), as well as the surveys cited in the previous footnote.

institutions, rely on voting to influence firms’ policies.<sup>11</sup> [Dhillon and Rossetto \(2015\)](#), [Bar-Isaac and Shapiro \(2020\)](#), and [Meirowitz and Pi \(2021\)](#) also consider blockholder models with voting, but differently from our paper, they do not study the voting premium and focus on the effects of blockholders on, respectively, the risk taking of the firm and information aggregation.

More broadly, our paper is related to an earlier literature on the existence of equilibrium and the objectives of the firm in a context with incomplete markets and shareholders with heterogeneous preferences.<sup>12</sup> In particular, [Drèze \(1985\)](#) and [DeMarzo \(1993\)](#) develop models with the board of directors as a group of controlling blockholders. To this literature, we contribute by analyzing the voting premium and a richer characterization of the interplay between small shareholders and blockholders. This also distinguishes our paper from [Levit, Malenko, and Maug \(2020\)](#), who analyze trading and voting by atomistic shareholders – a setting in which the voting premium does not arise.

### 3 Model

Consider a publicly traded firm, which is initially owned by a continuum of measure one of dispersed shareholders and one large blockholder. The blockholder is endowed with  $\alpha \in [0, 1)$  shares, and each dispersed shareholder is endowed with  $e = 1 - \alpha$  shares, so the total number of outstanding shares is 1. In the baseline setting, each share has one vote. There is a proposal on which shareholders vote. The proposal could relate to director elections, M&As, executive compensation, corporate governance, or social and environmental policies. The proposal can either be approved ( $d = 1$ ) or rejected ( $d = 0$ ).

**Preferences.** Shareholders’ preferences over the proposal depend on two components, which reflect a common value and private values. The common value component depends on an unknown state  $\theta \in \{-1, 1\}$ : if  $\theta = -1$  ( $\theta = 1$ ), accepting the proposal is value-decreasing (increasing). In other words, the common value is maximized if the policy matches the state ( $d = 1$  if  $\theta = 1$ ), as common in the strategic voting literature (e.g., [Austen-Smith and Banks \(1996\)](#) and [Feddersen and Pesendorfer \(1996\)](#)).

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<sup>11</sup>Thus, our paper contributes to the broader literature on corporate voting (e.g., [Maug and Rydqvist, 2009](#); [Levit and Malenko, 2011](#); [Van Wesep, 2014](#); [Malenko and Malenko, 2019](#); and [Cvijanovic, Groen-Xu, and Zachariadis, 2020](#)).

<sup>12</sup>See [Gevers \(1974\)](#), [Drèze \(1985\)](#), [DeMarzo \(1993\)](#), and [Kelsey and Milne \(1996\)](#).

Shareholders also have private values from the proposal, which reflect the heterogeneity in their preferences. For simplicity, we refer to these private values as biases and denote them by  $b$ . A shareholder with bias  $b > 0$  ( $b < 0$ ) receives additional (dis)utility if the proposal is accepted. The distribution of biases  $b$  among the initial dispersed shareholders is given by a publicly known differentiable cdf  $G$ , which has full support with a positive differentiable density function  $g$  on  $[-\bar{b}, \bar{b}]$ , where  $\bar{b} \in (0, 1)$ . Differences in shareholders' preferences can stem from time horizons, tax considerations, private benefits, social or political views, common ownership, or risk aversion, and we expand on some of these sources of heterogeneity at the end of this section. As noted in the introduction, the evidence for preference heterogeneity is pervasive.

The value of a share from the perspective of a dispersed shareholder with bias  $b$  is

$$v(d, \theta, b) = v_0 + (\theta + b)d, \tag{1}$$

where  $v_0 \geq 0$  ensures that shareholder value is always non-negative. Notice that because of heterogeneous preferences, shareholders apply different hurdle rates for accepting the proposal: a shareholder with bias  $b$  would like the proposal to be accepted if and only if his expectation of  $\theta + b$  is positive. We will refer to shareholders with a higher  $b$  as being “more activist”.

The blockholder's preferences have the same structure as those of dispersed shareholders, except that his bias is  $\beta \in [-\bar{b}, \bar{b}]$ . Thus, the value of a share from the perspective of a blockholder is  $v(d, \theta, \beta)$ .

**Timeline.** All shareholders are initially uninformed about the state  $\theta$  and have the same prior about its distribution, which we specify below. Shareholders first trade and then vote on the proposal. This timing allows us to focus on how trading affects the composition of the voter base, which is crucial for the analysis of the voting premium. At the trading stage, each dispersed shareholder can buy any number of shares  $x$ , where  $x < 0$  corresponds to the shareholder selling shares. A dispersed shareholder's utility from buying  $x$  shares is

$$u(d, \theta, b, x; \gamma, e) = (e + x)v(d, \theta, b) - \frac{\gamma}{2}x^2, \tag{2}$$

where  $\gamma > 0$  captures trading frictions, such as illiquidity, transaction costs, or wealth con-

straints, which limit shareholders' ability to build large positions in the firm.<sup>13</sup> Since the mass of investors is bounded and  $\gamma > 0$ , our model features limits to arbitrage.

Similarly, the blockholder can buy any number of shares  $y$ , and his utility from buying  $y$  shares is  $u(d, \theta, \beta, y; \eta, \alpha)$ , where  $u(\cdot)$  is given by (2) and  $\eta \geq 0$  captures the blockholder's trading costs. All results hold for  $\eta = 0$ . For simplicity, we assume that the blockholder submits his order  $y$  first, and dispersed shareholders observe  $y$  and submit their orders next. Effectively, dispersed shareholders trade shares by submitting limit orders.<sup>14</sup> Finally, we assume that neither dispersed shareholders nor the blockholder find it in their best interest to short sell.<sup>15</sup>

We denote the market clearing share price by  $p$ . After the market clears, but before voting takes place, all shareholders observe a public signal about the state  $\theta$ , which may stem from disclosures by management, proxy advisors, or analysts.<sup>16</sup> Let  $q = \mathbb{E}[\theta | \text{public signal}]$  be the shareholders' posterior expectation of the state following the signal. For simplicity, we assume that the public signal is  $q$  itself, and that  $q$  is distributed according to a differentiable cdf  $F$  with mean zero and full support with a positive differentiable density function  $f$  on  $[-\Delta, \Delta]$ , where  $\Delta \in (\bar{b}, 1)$ . Thus, the ex-ante expectation of  $\theta$  is zero. The symmetry of the support of  $q$  around zero is not necessary for any of the main results. In what follows, we refer to  $H(q^*) \equiv \Pr[q > q^*]$ , rather than to the cdf.

After observing the public signal  $q$ , each shareholder votes the shares he owns after the trading stage. Hence, we assume that the record date, which determines who is eligible to participate in the vote, is after the trading stage. This timeline applies well to important votes, such as the votes on M&As, proxy fights, and high-profile shareholder proposals, which are typically known well ahead of the record date. The proposal is accepted if at least fraction  $\tau \in (0, 1)$  of all shares are cast in favor; otherwise, the proposal is rejected. We assume that the

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<sup>13</sup>Since each dispersed investor has a zero mass, his trade  $x$  and endowment  $e$  are infinitesimal quantities. With a slight abuse of notation,  $e$  also denotes the total endowment held by dispersed investors.

<sup>14</sup>As equation (33) shows, if  $\gamma$  is sufficiently large, then the market clearing price is monotonic in  $y$ , and thus, whether the limit order is conditioned on the price itself or the blockholder's trade is immaterial for our analysis.

<sup>15</sup>Lemma 3 in the Online Appendix shows that if  $\alpha > 0$  and  $\gamma$  is sufficiently large, then there are no short sales in equilibrium. If  $\alpha = 0$ , which we analyze as a special case and separately from Proposition 2, the no-short-selling constraint can bind for the blockholder, but it does not change our main results.

<sup>16</sup>In practice, proxy advisors' recommendations (and management's response) are on average released about one month after the record date. See, for example, Fig. 1 in Li, Maug, and Schwartz-Ziv (2022).

blockholder’s initial stake and ability to buy shares are not large enough to grant him the power to accept the proposal unilaterally, as well as to veto the proposal, i.e.,  $\alpha + y < \min \{\tau, 1 - \tau\}$  in any equilibrium.<sup>17</sup>

We analyze subgame perfect Nash equilibria in undominated strategies of the voting game. The restriction to undominated strategies is common in voting games, which usually impose the equivalent restriction that dispersed shareholders vote as-if-pivotal.<sup>18</sup> This implies that an investor with bias  $b$ , whether he is a dispersed shareholder or the blockholder, votes in favor of the proposal if and only if

$$b + q > 0. \tag{3}$$

**Applications of the model.** Several applications can be mapped into our model (see Section B of the Online Appendix). In the first application, we consider investors with heterogeneous time horizons who vote between a short-termist and a long-termist investment strategy, such as in a proxy contest organized by a short-termist activist. Shareholders’ valuations of the firm under each strategy depend on the likelihood that the strategy succeeds (common value) and on their time horizons (private values): long-termist shareholders put a higher weight on long-term cash flows relative to short-term cash flows. In this application, shareholders’ trading and voting strategies, as well as the voting premium, are given by the same expressions (up to a constant) as in the baseline model.

In the second application we microfound shareholders’ valuations in eq. (1) via a model in which biases  $b$  and  $\beta$  capture differences in beliefs (“sentiment”) regarding the value of the proposal, rather than differences in preferences. The third application captures a setting with private benefits of control. The blockholder can dilute the assets of the firm if the proposal is approved, which leads him to favor the proposal relative to dispersed shareholders ( $\beta > b$ ). Finally, the fourth application captures costly monitoring: if the proposal is approved, the blockholder can monitor the manager and increase firm value at a private cost. Since dispersed shareholders benefit from monitoring but do not incur its cost, they favor the proposal more than the blockholder ( $b > \beta$ ).

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<sup>17</sup>Lemma 3 in the Online Appendix shows that if  $\alpha < \min \{\tau, 1 - \tau\}$  and  $\gamma$  is sufficiently large, then  $\alpha + y < \min \{\tau, 1 - \tau\}$  in any equilibrium.

<sup>18</sup>See, e.g., [Baron and Ferejohn \(1989\)](#) and [Austen-Smith and Banks \(1996\)](#). This restriction helps rule out trivial equilibria, in which shareholders are indifferent between voting for and against because they are never pivotal.

## 4 Equilibrium

We begin by showing that for any trading outcome, proposal approval at the voting stage takes the form of a cutoff decision rule:

**Lemma 1.** *In any equilibrium, there exists  $q^*$  such that the proposal is approved if and only if  $q > q^*$ .*

The reason is that all shareholders value the proposal more if it is more likely to be value-increasing, i.e., if  $\theta = 1$  is more likely.

We proceed in several steps. First, for any possible blockholder's trade  $y$ , Sections 4.1 and 4.2 characterize the trading of dispersed shareholders and the voting stage as a function of  $y$ . In Section 4.3, we solve for the optimal trade of the blockholder,  $y^*$ , and for the equilibrium share price.

### 4.1 Trading of dispersed shareholders

Given Lemma 1, suppose that dispersed shareholders expect the proposal to be accepted if and only if  $q > q_e^*$  for some cutoff  $q_e^*$  (we later derive the equilibrium cutoff such that shareholders' expectations are rational). Let  $v(b, q_e^*)$  denote the valuation of a shareholder with bias  $b$  prior to the realization of  $q$ , as a function of the cutoff  $q_e^*$ . Then

$$v(b, q_e^*) = \mathbb{E} [v(\mathbf{1}_{q > q_e^*}, \theta, b)], \quad (4)$$

where the indicator function  $\mathbf{1}_{q > q_e^*}$  equals one if  $q > q_e^*$  and zero otherwise, and  $v(d, \theta, b)$  is defined by (1). We can rewrite (4) as

$$v(b, q_e^*) = v_0 + (b + \mathbb{E}[\theta | q > q_e^*]) H(q_e^*), \quad (5)$$

which increases in  $b$ . Dispersed shareholders are price takers, so for any share price  $p$ , each dispersed shareholder solves

$$\max_x \left\{ (e + x) v(b, q_e^*) - xp - \frac{\gamma}{2} x^2 \right\} \quad (6)$$

and optimally chooses

$$x(b, q_e^*, p) = \frac{v(b, q_e^*) - p}{\gamma}. \quad (7)$$

Thus, shareholder  $b$  buys shares if his valuation exceeds the market price,  $v(b, q_e^*) > p$ , sells shares if  $v(b, q_e^*) < p$ , and does not trade otherwise. Given the blockholder's order  $y$ , the market clears if and only if

$$\int_{-\bar{b}}^{\bar{b}} x(b, q_e^*, p) g(b) db + y = 0, \quad (8)$$

which gives the market clearing price

$$p^*(y, q_e^*) = \gamma y + v(\mathbb{E}[b], q_e^*). \quad (9)$$

The equilibrium share price increases in  $y$ , and the price impact of the blockholder's trade is larger if  $\gamma$  is larger. Thus, we can interpret  $\gamma$  as measuring the illiquidity of the market, i.e., the inverse of  $\gamma$  reflects market depth. In addition, the share price (9) increases in the valuation of the average dispersed shareholder. Intuitively, if dispersed shareholders' valuations (conditional on  $q_e^*$ ) are higher, they are willing to supply shares to the blockholder only at a higher price.

From (5), (7), and (9), dispersed shareholders' demand as a function of the blockholder's trade can be written as

$$x(b, y, q_e^*) = \frac{1}{\gamma} (b - \mathbb{E}[b]) H(q_e^*) - y. \quad (10)$$

**The post-trade ownership structure.** Next, we characterize the post-trade ownership structure. After the trading stage, the blockholder owns  $\alpha + y$  shares, a dispersed shareholder with bias  $b$  owns  $1 - \alpha + x(b, y, q_e^*)$  shares, and all dispersed shareholders collectively own  $1 - \alpha - y$  shares. Thus, the proportion of shares owned post-trade by dispersed shareholders with bias  $b$ , conditional on the expected decision rule  $q_e^*$  and blockholder's trade  $y$ , is given by

$$r(b; y, q_e^*) \equiv g(b) \frac{1 - \alpha + x(b, y, q_e^*)}{1 - \alpha - y}. \quad (11)$$

Note that  $r(b; y, q_e^*)$  is a density function, i.e.,  $\int_{-\bar{b}}^{\bar{b}} r(b; y, q_e^*) db = 1$ . Thus, the post-trade dispersed shareholder base is characterized by the cdf  $R(b; y, q_e^*)$  given by

$$\begin{aligned} R(b'; y, q_e^*) &= \int_{-\bar{b}}^{b'} r(b; y, q_e^*) db \\ &= G(b') \left( 1 - \frac{\mathbb{E}[b] - \mathbb{E}[b|b < b']}{\gamma} \frac{H(q_e^*)}{1 - \alpha - y} \right), \end{aligned} \quad (12)$$

where the second equality follows from (10) and (11). The cdf  $R$  characterizes the post-trade dispersed shareholder base, whereas  $G$  characterizes the pre-trade dispersed shareholder base. Note that  $R(b) < G(b)$  for any  $b$ , i.e.,  $R$  dominates  $G$  in the sense of first-order stochastic dominance. Hence, trading shifts the shareholder base in such a way that more activist shareholders own a larger proportion of the firm after trading. Moreover,  $R(b'; y, q_e^*)$  increases in  $q_e^*$ ; hence, a more activist decision rule (lower  $q_e^*$ ) makes the post-trade shareholder base more activist. Intuitively, shareholders' heterogeneous attitudes towards the proposal create gains from trade, so the shareholder base moves in the direction of the expected outcome.

## 4.2 Voting

The composition of the post-trade shareholder base determines the voting outcome. We first analyze the votes of dispersed shareholders. Denote by  $s(q; y, q_e^*)$  the number of votes cast by dispersed shareholders in favor of the proposal if signal  $q$  is realized, the blockholder traded  $y$  shares, and the expected decision rule is  $q_e^*$ . Then,

$$s(q; y, q_e^*) \equiv (1 - \alpha - y) (1 - R(-q; y, q_e^*)), \quad (13)$$

which is the number of shares held by dispersed shareholders,  $1 - \alpha - y$ , multiplied by the proportion of dispersed shareholders for whom  $b > -q$ .

The blockholder is pivotal for the outcome only if at least  $\tau - (\alpha + y)$  but no more than  $\tau$  dispersed shareholders vote to support the proposal, i.e., if and only if

$$\tau - (\alpha + y) < s(q; y, q_e^*) < \tau. \quad (14)$$

Otherwise, if  $s(q; y, q_e^*) < \tau - (\alpha + y)$  ( $s(q; y, q_e^*) \geq \tau$ ), the proposal fails (succeeds) inde-



pendently of the vote of the blockholder. From (13), the support of dispersed shareholders is increasing in the signal  $q$ . Define the bounds  $\underline{q} \equiv s^{-1}(\tau - \alpha - y; y, q_e^*)$  and  $\bar{q} \equiv s^{-1}(\tau; y, q_e^*)$ , so that the blockholder is pivotal whenever the signal is in the intermediate range  $q \in [\underline{q}, \bar{q}]$ . If  $q < \underline{q}$  ( $q > \bar{q}$ ), dispersed shareholders' support for the proposal is so low (high) that the proposal fails (succeeds) even if the blockholder supports (rejects) it.

We describe the voting outcome by characterizing the identity of the *median voter*, who is defined as the shareholder whose individual vote always coincides with the collective decision on the proposal. In other words, whenever the median voter votes in favor (against), the proposal is accepted (rejected). Let  $b_{MV}(\beta, y, q_e^*)$  denote the bias of the median voter if the expected decision rule is  $q_e^*$ , the blockholder traded  $y$  shares, and his bias is  $\beta$ . There are three possible cases, which define  $b_{MV}(\beta, y, q_e^*)$ :

- (i) If  $\beta > -\underline{q}$ , the blockholder is very activist and supports the proposal whenever he is pivotal. The proposal is accepted if and only if  $s(q; y, q_e^*) + \alpha + y \geq \tau$ , i.e., whenever  $q \geq \underline{q}$ . Hence, the proposal passes if and only if the dispersed shareholder with bias  $b = -\underline{q}$  votes in favor. This shareholder is then the median voter, i.e.,  $b_{MV}(\beta, y, q_e^*) = -\underline{q}$ .
- (ii) If  $\beta < -\bar{q}$ , the blockholder has a large bias against the proposal and votes against whenever he is pivotal. The proposal is accepted if and only if  $s(q; y, q_e^*) \geq \tau$ , i.e., whenever  $q \geq \bar{q}$ . Hence, the proposal passes if and only if the dispersed shareholder with bias  $b = -\bar{q}$  votes in favor. This shareholder is then the median voter, i.e.,  $b_{MV}(\beta, y, q_e^*) = -\bar{q}$ .
- (iii) If  $-\bar{q} < \beta < -\underline{q}$ , the blockholder is pivotal if  $q \in [\underline{q}, \bar{q}]$  and votes in favor if and only if  $q \geq -\beta$ . Then, the proposal is accepted if and only if the blockholder votes in favor, so the blockholder is the median voter,  $b_{MV}(\beta, y, q_e^*) = \beta$ .

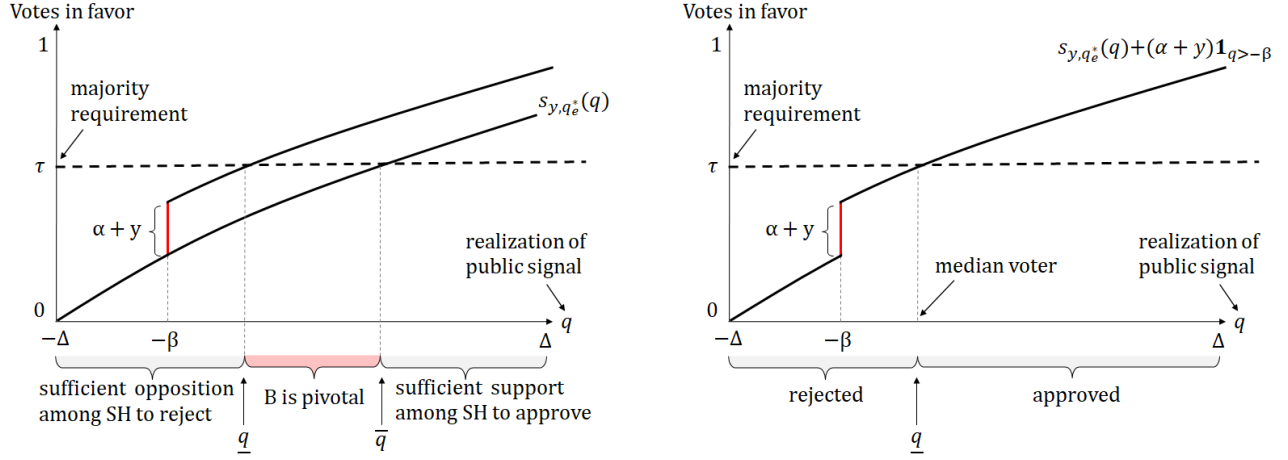


Figure 1 - The pivotal voter and the median voter

We conclude that if shareholders anticipate decision rule  $q_e^*$  when trading, then the decision rule at the voting stage is characterized by the three cases above. The first case is illustrated in Figure 1, which plots the number of votes in favor of the proposal as a function of the signal  $q$ . The left panel indicates the range in which the blockholder is pivotal; the right panel indicates the approval range and the location of the median voter.

The distinction between the pivotal voter and the median voter is an important implication of this argument. A voter is pivotal if his vote can sway the decision on the proposal. Only the blockholder can be pivotal in our setting, since all other shareholders are atomistic. In contrast, the median voter is the shareholder whose vote always coincides with the decision on the proposal. In the first two cases above, the blockholder is extreme and the median voter is a dispersed shareholder closer to the center of the distribution of votes. The distinction between the median voter and the pivotal voter will play a key role in our analysis of the voting premium (see Section 5).

In equilibrium, shareholders' expectations  $q_e^*$  must be consistent with the actual decision rule. Hence, an equilibrium can be found as a fixed point of  $q_e^*$ , such that  $-b_{MV}(\beta, y, q_e^*) = q_e^*$ , where  $b_{MV}(\beta, y, q_e^*)$  is defined by the three cases above. Using this logic, the equilibrium at the voting stage is characterized as follows.

**Proposition 1 (Voting stage).** *If the blockholder trades  $y$  shares, then the proposal is ap-*

proved if and only if  $q > q^*(y)$ , where  $q^*(y)$  solves

$$-b_{MV}(\beta, y, q^*) = q^*. \quad (15)$$

There exists  $\bar{\gamma} < \infty$  such that if  $\gamma > \bar{\gamma}$ , the solution of (15) is unique. In this case, there exists  $\bar{y}$  such that if  $y > \bar{y}$ , the median voter is the blockholder ( $-q^*(y) = \beta$ ), whereas if  $y < \bar{y}$ , the median voter is a dispersed shareholder with bias  $-q^*(y) \neq \beta$ , and  $|\beta + q^*(y)|$  decreases in  $y$ .

In general, there can be multiple solutions to (15), and hence multiple equilibria at the voting stage. This is because for small  $\gamma$ , the shifts in the shareholder base are sensitive to the expected decision rule  $q_e^*$ , which can give rise to self-fulfilling expectations.<sup>19</sup> However, if  $\gamma$  is large enough, then dispersed shareholders trade less aggressively, the distribution of the post-trade shareholder base is less sensitive to  $q_e^*$ , and the equilibrium is unique. From this point on, we focus on parameterizations for which the equilibrium at the voting stage is unique.

Importantly, Proposition 1 shows that the blockholder can change the identity of the median voter,  $-q^*(y)$ , and thus the vote outcome, with his trades  $y$ . By buying more shares, the blockholder moves the bias of the median voter closer to  $\beta$ , as captured by the result that  $|\beta + q^*(y)|$  decreases. This can be seen in the left panel of Figure 2, which shows that a larger  $y$  pushes  $-q^*(y)$  to the left, closer to  $-\beta$ . Once the blockholder buys enough shares ( $y > \bar{y}$ ), the vote outcome exactly coincides with the blockholder's own voting rule, so the blockholder becomes the median voter (see the right panel in Figure 2). The accumulation of shares beyond  $\bar{y}$  increases the probability of the blockholder being pivotal, but does not change the expected vote outcome, that is, the identity of the median voter.

There are two complementary reasons why the accumulation of shares by the blockholder moves the median voter closer to him. First, more shares give the blockholder more voting power. Second, as the blockholder buys more, the composition of the dispersed shareholder base changes towards those who are more aligned with the blockholder. For example, if the blockholder is very activist, then dispersed shareholders who hold the firm after trading are

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<sup>19</sup>In particular, the cdf of the post-trade shareholder base, given by (12), increases in  $q_e^*$ , and hence a more activist *expected* decision rule (lower  $q_e^*$ ) makes the post-trade shareholder base more activist. A more activist shareholder base, in turn, is more likely to approve the proposal for any given signal, leading to a lower *realized* cutoff for approving the proposal, confirming the ex-ante expectations.

more activist. (Recall that  $R(b'; y, q_e^*)$  increases in  $q_e^*$  in (12).)

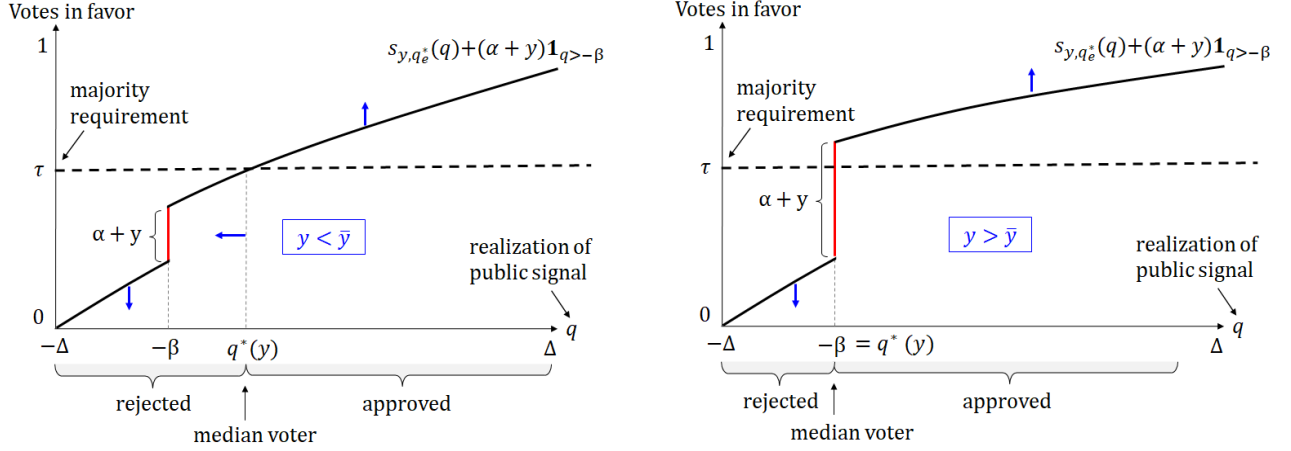


Figure 2 - The effect of the blockholder's trade on the equilibrium median voter

### 4.3 Blockholder trading

Given the blockholder's trade  $y$ , all shareholders correctly anticipate that the decision rule at the voting stage will be  $q^*(y)$ , as given by (15), and that the market clearing price will be

$$p^*(y) = \gamma y + v(\mathbb{E}[b], q^*(y)) \quad (16)$$

from (9). In equilibrium, the blockholder chooses  $y$  to maximize

$$\Pi(y) \equiv (\alpha + y)v(\beta, q^*(y)) - yp^*(y) - \frac{\eta}{2}y^2. \quad (17)$$

The marginal effect of buying additional shares on the blockholder's expected payoff is

$$\frac{d\Pi(y)}{dy} = \underbrace{\frac{\partial \Pi(y)}{\partial y}}_{MPC(y)} + \underbrace{\frac{\partial \Pi(y)}{\partial (-q^*(y))} \frac{\partial (-q^*(y))}{\partial y}}_{MPV(y)} = MPC(y) + MPV(y). \quad (18)$$

The term  $MPC(y)$  is the *marginal payoff from buying cash flow rights*. It can be thought of as the blockholder's marginal payoff from trading in a hypothetical scenario in which the decision rule is set exogenously at the level  $q^*(y)$  and is not affected by the blockholder's trades. This term equals

$$MPC(y) = (\beta - \mathbb{E}[b])H(q^*(y)) - (2\gamma + \eta)y. \quad (19)$$

Intuitively, if  $\beta > \mathbb{E}[b]$  ( $\beta < \mathbb{E}[b]$ ), the blockholder values shares more (less) than the average dispersed shareholder, which creates gains from trade. The term  $MPV(y)$  is the *marginal payoff from buying voting rights*. It captures the blockholder's additional incentives to trade in order to change the decision rule, i.e., to shift the median voter  $-q^*(y)$ . In Section 5 below, we show that  $MPV(y)$  is closely connected to the voting premium.

The next proposition characterizes the equilibrium, including the blockholder's optimal trading strategy. As before, we focus on the case when the equilibrium is unique and, accordingly, assume that  $\gamma$  is large enough.

**Proposition 2 (Equilibrium).** *Suppose the blockholder has an endowment  $\alpha > 0$ . There exists  $\bar{\gamma} < \infty$  such that if  $\gamma > \bar{\gamma}$ , the equilibrium exists and is unique. In this equilibrium:*

(i) *The blockholder trades  $y^*$  shares, where*

$$y^* = \frac{1}{2\gamma + \eta} (\beta - \mathbb{E}[b]) H(q^*(y^*)) + \frac{1}{2\gamma + \eta} MPV(y^*), \quad (20)$$

*and a dispersed shareholder with bias  $b$  trades  $x^*(b)$  shares, where*

$$x^*(b) = \frac{1}{\gamma} (b - b^*) H(q^*(y^*)) - \frac{1}{2\gamma + \eta} MPV(y^*) \quad (21)$$

*and*

$$b^* = \frac{\gamma}{2\gamma + \eta} \beta + \left(1 - \frac{\gamma}{2\gamma + \eta}\right) \mathbb{E}[b]. \quad (22)$$

(ii) *The share price is*

$$p^* = v(b^*, q^*(y^*)) + \frac{\gamma}{2\gamma + \eta} MPV(y^*). \quad (23)$$

(iii) *The bias of the median voter is  $-q^*(y^*)$ , where  $q^*(\cdot)$  is defined in Proposition 1.*

The blockholder's optimal trade  $y^*$  consists of two terms, which are related to decomposition (18). The first term reflects trading for cash flow reasons: the blockholder has an incentive to buy shares if and only if his valuation is higher than that of the average dispersed shareholder,  $\beta > \mathbb{E}[b]$ . The second term reflects the additional trading of voting shares because of the embedded voting rights and is proportional to  $MPV(y^*)$ . The expression for dispersed shareholders' trades  $x^*(b)$  follows directly from (10). Intuitively, trading shifts the dispersed

shareholder base towards the expected outcome (see the discussion after eq. (12) above), and their combined supply of shares equals the blockholder's demand. If  $MPV(y^*) = 0$ , then the shareholder with bias  $b^*$  can be interpreted as the marginal trader who is indifferent between buying and selling shares at the equilibrium share price; in this scenario, all shareholders with a higher (lower)  $b$  than  $b^*$  buy (sell) shares. Finally, the equilibrium stock price consists of two terms, and we focus on this decomposition and its properties in the next section.

## 5 The voting premium

This section presents our main results. We proceed in several steps. We define the voting premium in Section 5.1 and clarify its determinants in Section 5.2. In Section 5.3 we characterize the equilibrium properties of the voting premium. Finally, in Section 5.4 we discuss the novel implications about the voting premium that emerge from our analysis.

### 5.1 Defining the voting premium

We start by defining the voting premium and relating it to  $MPV$ . Consider again the hypothetical scenario in which the voting rule is set exogenously at  $q^*(y^*)$ . Such a scenario may reflect cases in which trading does not reallocate voting rights among investors, so the median voter is unaffected.<sup>20</sup> Since the voting rule is exogenous in this hypothetical scenario, we have  $\frac{\partial(-q^*(y^*))}{\partial y} = 0$ ,  $MPV(y^*) = 0$ , and the blockholder's first-order condition (18) reduces to  $MPC(y^*) = 0$ . A corollary of Proposition 2 shows that the share price in this scenario reflects the valuation of the shareholder with bias  $b^*$ , defined in (22):

**Corollary 1** *If the voting rule is set exogenously at  $q^*(y^*)$ , the equilibrium share price is given*

$$p_{CF}(q^*(y^*)) = v(b^*, q^*(y^*)). \quad (24)$$

Next, we define the *voting premium* as

$$VP(y^*) \equiv p^* - p_{CF}(q^*(y^*)), \quad (25)$$

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<sup>20</sup>This hypothetical scenario also captures cases in which the company's board and management have decision rights over the proposal and implement a decision rule  $q^*(y^*)$  that is exogenous to the composition of the shareholder base.

i.e., the difference between the share price (23) that arises when the voting rule is determined endogenously by the post-trade shareholder base, and the share price in the hypothetical scenario when the voting rule is set exogenously at the same level  $q^*(y^*)$ . Proposition 2 and Corollary 1 imply that the voting premium is proportional to the blockholder’s marginal payoff from buying voting rights:

$$VP(y^*) = \frac{\gamma}{2\gamma + \eta} MPV(y^*). \quad (26)$$

Hence, the voting premium reflects the additional component of the stock price that arises from the blockholder’s incentive to influence the voting outcome.

There are two empirical counterparts of our definition of the voting premium. First, we can think of it as the difference between the stock prices right before and after the record date (Fos and Holderness (2020)). These prices reflect the same expected voting rule, but shares traded right before the record date have voting rights for the upcoming shareholder meeting, whereas shares traded right after the record date do not.<sup>21</sup> The second empirical counterpart is the *dual-class premium*, which we formalize in an extension to a dual-class share structure in Section 6.<sup>22</sup> However, our definition of the voting premium is broader than these two empirical measures and suggests a way to isolate the voting premium as a component of the stock price also in single-class firms and on dates other than the record date.

## 5.2 Determinants of the voting premium

To understand the determinants of the voting premium, we rewrite (26), using (18), as

$$VP(y) = \underbrace{\frac{\partial(-q^*(y))}{\partial y}}_{\text{ability to move median voter}} \times \underbrace{\left[ (\alpha + y) \frac{\partial v(\beta, q^*(y))}{\partial(-q^*)} - y \frac{\partial p^*(y)}{\partial(-q^*)} \right]}_{\substack{\text{marginal benefit of a vote} \\ \text{price impact of a vote}}} \times \frac{\gamma}{2\gamma + \eta}. \quad (27)$$

incentives to move median voter =  $\frac{\partial \Pi(y)}{\partial(-q^*(y))}$

<sup>21</sup>Our model is static in nature, so our analogy to trades around the record date abstracts from dynamic aspects of trade that could potentially affect the share price.

<sup>22</sup>Empirical estimates of the dual-class premium go back at least to Lease, McConnell, and Mikkelsen (1983) and Levy (1983). See Adams and Ferreira (2008) for a survey of the earlier literature and Bigelli and Croci (2013), ?, and ? for more recent contributions.

Thus, the voting premium can be decomposed into the blockholder's *ability* to influence the identity of the median voter, and his *incentives* to do so.

The ability of the blockholder to influence the median voter depends on how his trades  $y$  affect  $-q^*(y)$ . According to Proposition 1, there exists  $\bar{y}$  such that if  $y > \bar{y}$ , then the blockholder is the median voter and the accumulation of additional shares does not change it. Therefore, if  $y > \bar{y}$ , then  $\frac{\partial(-q^*(y))}{\partial y} = 0$  and the blockholder cannot change the voting outcome even if he had the incentives to do so. According to (27), the voting premium is then zero. Intuitively, since the blockholder's trades have no impact on the voting outcome, he would not be willing to pay a premium for additional voting rights.

Proposition 1 also shows that if  $y < \bar{y}$ , then  $\frac{\partial(-q^*(y))}{\partial y} \neq 0$  and the blockholder's trades change the identity of the median voter. In this case, the voting premium also depends on the incentives of the blockholder to move the median voter. Based on (27), these incentives consist of two components. The first component captures how a marginal change in the median voter affects the blockholder's valuation of his post-trade stake in the firm,  $\alpha + y$ , and we refer to it as the *marginal benefit of a vote*. From (5) and (27),

$$\text{Marginal benefit of a vote} = (\alpha + y) \frac{\partial v(\beta, q^*(y))}{\partial(-q^*)} = (\alpha + y) (\beta + q^*(y)) f(q^*(y)). \quad (28)$$

By buying additional shares, the blockholder moves the median voter  $-q^*(y)$  closer to his own bias  $\beta$  (see Proposition 1), which increases the blockholder's valuation of his stake. Thus, the blockholder always values a marginal vote for its impact on his stake, that is, the marginal benefit of a vote is always positive.<sup>23</sup>

The second component captures the blockholder's additional incentives to move the median voter due to the associated *price impact*, which in turn affects the blockholder's gains from trade. Based on (16), the effect of a marginal change in the median voter  $-q^*$  on the stock price is

$$\text{Price impact of a vote} = \frac{\partial p^*(y)}{\partial(-q^*)} = (\mathbb{E}[b] + q^*(y)) f(q^*(y)). \quad (29)$$

The sign and magnitude of the price impact of a vote depend on  $\mathbb{E}[b]$ , the bias of the average

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<sup>23</sup>The discussion above simplifies by focusing on the case in which the blockholder is sufficiently activist, such that  $\beta > -q^*(y)$  and (28) is positive. In the opposite case, in which  $\beta < -q^*(y)$  and (28) is negative, the derivative  $\frac{\partial(-q^*(y))}{\partial y}$  turns negative as well, so that the product of both expressions in (27) remains positive: The marginal benefit of a vote is always positive. Hence, our simplification is inconsequential.



dispersed shareholder. Intuitively, the market clearing price reflects the reservation price at which dispersed shareholders are willing to supply their shares, so the price impact of a vote depends on whether the resulting change in the median voter benefits or hurts dispersed shareholders. The sign of this effect is generally ambiguous and we discuss it in detail in Section 5.4.4.

### 5.3 Properties of the voting premium

The discussion in Section 5.2 highlights that a key determinant of the voting premium is the location of the median voter. The next result characterizes the equilibrium median voter and the voting premium as functions of the blockholder's bias  $\beta$ .

**Proposition 3** *For every  $\gamma > \bar{\gamma}$ , where  $\bar{\gamma}$  is defined by Proposition 2, there are cutoffs  $\underline{\beta} < \bar{\beta}$  such that:*

- (i) *If  $\beta \in [\underline{\beta}, \bar{\beta}]$ , then the median voter is the blockholder and the voting premium is zero.*
- (ii) *If  $\beta > \bar{\beta}$  ( $\beta < \underline{\beta}$ ), then the median voter is a dispersed shareholder with a smaller (larger) bias toward the proposal than the blockholder, i.e.,  $-q^*(y^*) < \beta$  ( $-q^*(y^*) > \beta$ ), and the voting premium is strictly positive and increases (decreases) in  $\beta$ .*

Figure 3 illustrates Proposition 3. The bold black curve plots the bias of the median voter and the blue curve plots the equilibrium voting premium, both as functions of the blockholder's bias. There are two distinct scenarios. First, if the blockholder is moderate,  $\beta \in (\underline{\beta}, \bar{\beta})$ , then he is the median voter himself; in Figure 3, the black curve coincides with the 45-degree line. In this region, the blockholder's ability to move the median voter is zero at the margin; consequently, the voting premium is also zero. This observation further highlights that it is the median voter, and not the pivotal voter, that affects the voting premium (see Section 4.2).

Second, if the blockholder's preferences are more extreme,  $\beta > \bar{\beta}$  (or  $\beta < \underline{\beta}$ ), then the blockholder does not become the median voter. Then the median voter is a dispersed shareholder with a smaller (larger) bias toward the proposal than the blockholder, and the black curve is below (above) the 45-degree line. Now the blockholder does have the ability to move the median voter, and he benefits more from doing so if he is further away from the median

voter. Accordingly, the voting premium is positive and increases as  $\beta$  becomes more extreme. Importantly, even though the blockholder's net marginal benefit of a vote is positive, he refrains from buying more voting shares, because he also cares about his gains from trade.

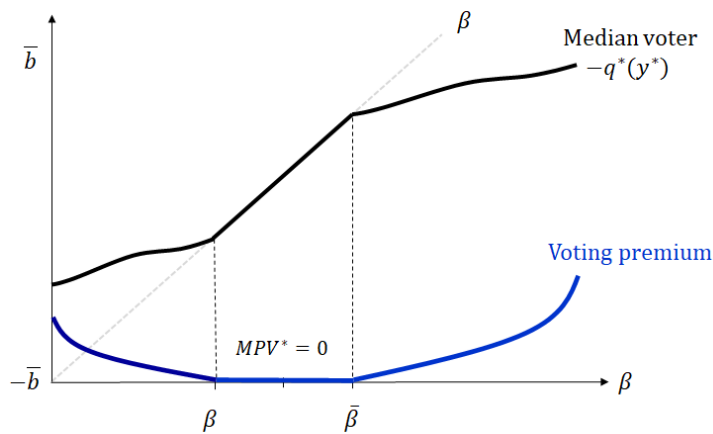


Figure 3 - Equilibrium median voter and voting premium.

## 5.4 Implications

In this section we discuss the key implications of our analysis of the voting premium.

### 5.4.1 Voting premium vs. total value of voting rights

Our analysis highlights that the voting premium is likely to *underestimate* the overall value of voting rights. A zero voting premium does not imply that the blockholder does not value voting rights, or that he would not benefit from further influencing the voting outcome. Indeed, the incentives to move the median voter, captured by  $\frac{\partial \Pi(y)}{\partial (-q^*)}$ , will generally differ from zero, even if the blockholder is already the median voter.<sup>24</sup> Instead, a zero voting premium only implies that the blockholder cannot influence the position of the median voter through additional trades.

Furthermore, the blockholder's overall benefits from accumulating voting rights can be positive even if his marginal benefits are zero, because these marginal benefits are evaluated at the blockholder's equilibrium trade  $y^*$ . By contrast, the overall benefits from owning voting rights also come from the blockholder's infra-marginal trades. These infra-marginal trades

<sup>24</sup>To see this, note that if  $-q^*(y) = \beta$ , then  $\frac{\partial \Pi(y)}{\partial (-q^*)} = y(\beta - \mathbb{E}[b])f(-\beta)$ , which generally differs from zero. Intuitively, by changing the median voter further, the blockholder affects his gains from trade with small shareholders since the effect of the median voter on their valuations differs from the effect of the median voter on his own valuation (see Section 5.4.4 for a more in-depth discussion).

affect the voting outcome ( $q^*(y^*) \neq q^*(0)$ ), even if the equilibrium voting premium is zero. Hence, empirical measures of the voting premium that measure the value of a marginal vote, such as the dual-class premium or the ex-record date price drop, are likely to underestimate the overall value of voting rights.

#### 5.4.2 Direct vs. indirect influence on the voting outcome

The voting premium emerges not from the blockholder's accumulation of voting power, but from his indirect influence on the voting outcome through the composition of the shareholder base. In particular, the blockholder does not pay a voting premium for being directly in control of the voting outcome, and he never becomes a majority shareholder. Moreover, the voting premium is zero when the blockholder becomes the median voter, in which case the voting outcome is aligned with his bias. Instead, he pays the voting premium for influencing the identity of the dispersed shareholder who becomes the median voter.

As such, the voting premium is generally unrelated, or can even be negatively related, to measures of voting power. If the blockholder's voting power is large, he is the median voter himself, so the voting premium is zero. In contrast, if the blockholder's voting power is small, his marginal payoff from moving the median voter is strictly positive. He has both, the ability and, under the conditions of Proposition 2, also the incentives to do so; accordingly, the voting premium is positive as well.

#### 5.4.3 Conflicts of interest and the voting premium

**Divergence between the blockholder and small shareholders.** The literature often relates the voting premium to conflicts between majority blockholders and minority shareholders. The idea is that a large voting premium may be associated with a lower payoff of dispersed shareholders, since the blockholder exploits his voting power to advance his own agenda at the expense of others. In this section, we show that this intuition is not always correct.

We start by defining the aggregate equilibrium payoff of dispersed shareholders as

$$W^* \equiv \int_{-\bar{b}}^{\bar{b}} u^*(b) g(b) db, \quad (30)$$

where  $u^*(b)$  is the expected payoff of a dispersed shareholder with bias  $b$ :

$$u^*(b) = (e + x^*(b))v(b, q^*(y^*)) - x^*(b)p^* - \frac{\gamma}{2}x^*(b)^2, \quad (31)$$

and  $x^*(b)$ ,  $q^*(y^*)$ , and  $p^*$  are defined in Proposition 2. The next result shows how  $W^*$  is related to the voting premium.

**Proposition 4.** *Suppose the conditions of Proposition 2 are satisfied.*

- (i) *If  $\bar{\beta} \leq \mathbb{E}[b] < \beta$ , then both  $W^*$  and the voting premium strictly increase with  $\beta$ .*
- (ii) *Suppose  $\mathbb{E}[b] \leq \beta < \underline{\beta}$ .*
  - (a) *If  $\alpha > \underline{\alpha}$ , where  $\underline{\alpha}$  is defined in Lemma 4 in the Online Appendix, then both  $W^*$  and the voting premium strictly decrease with  $\beta$ .*
  - (b) *If  $\alpha$  is sufficiently small, then  $W^*$  strictly increases in  $\beta$ , whereas the voting premium strictly decreases with  $\beta$ .*

The striking result in Proposition 4 is that a change in  $\beta$  may be associated with both an increase in the voting premium and an increase in the payoff of small shareholders (parts (i) and (ii.a)). In other words, a larger voting premium does not necessarily indicate a greater conflict between the blockholder and small shareholders. To understand the intuition, note that  $W^*$  can be written as

$$W^* = ev(\mathbb{E}[b], q^*) + \frac{1}{2\gamma}\mathbb{E}[(v(b, q^*) - p^*)^2]. \quad (32)$$

The first term in (32) is dispersed shareholders' aggregate payoff from their endowment, whereas the second term reflects the aggregate gains from trade of dispersed shareholders, both among themselves and with the blockholder. To facilitate the explanation, we focus on the first term and abstract from trading profits.

Part (i) describes the case in which  $\beta > \bar{\beta}$ . If  $\gamma$  is large, as under the conditions of the proposition, then the median voter is approximately  $\bar{\beta}$ , and as the blockholder becomes more activist, he moves away from the median voter. This gives the blockholder stronger incentives to change the median voter and increases the voting premium (see Proposition 3). At the

same time,  $\bar{\beta} < \mathbb{E}[b]$  implies that the median voter is less activist than the average dispersed shareholder. Then, as the blockholder becomes more activist, his accumulation of voting shares moves the median voter closer to the average preferences of dispersed shareholders, increasing their payoff as well. As a result, the aggregate payoff of small shareholders and the voting premium move in the same direction.

There are two scenarios that can lead to such a situation. First, consider a setting with a simple majority requirement in which the post-trade distribution of dispersed shareholders' preferences is right-skewed. This means that more activist small shareholders feel much more strongly about the advantages of the proposal than their less activist peers. The median voter does not reflect this asymmetric intensity of preferences, but it is relevant for the payoff  $W^*$ , which is based on the average and not on the median payoff. Second, suppose that the post-trade distribution of preferences is symmetric, but the proposal is subject to a supermajority requirement ( $\tau > 0.5$ ). The supermajority requirement introduces a conservative bias into the voting process and thereby reduces the bias of the median voter.

In both scenarios, the voting rule is too conservative from the perspective of an average small shareholder. Then a more activist blockholder becomes a countervailing force against this conservative bias and increases the aggregate payoff of small shareholders. Notably, this happens even though the distance between the blockholder and the average small shareholder increases with  $\beta$ . Hence, what ultimately matters for small shareholders is not whether the blockholder is closer to them, but whether he moves the median voter closer to them.<sup>25</sup> At the same time, the increased distance between a more activist blockholder and the median voter increases the voting premium in both scenarios (Proposition 3).

Part (ii.a) describes the case symmetric to part (i), in which  $\beta < \underline{\beta}$ . The intuition in this case is the mirror image of the intuition for part (i) and is omitted for brevity. Finally, part (ii.b) gives sufficient conditions for the voting premium and the payoff of small shareholders to move in opposite directions. In this case, a larger voting premium is associated with a larger conflict between the blockholder and the small shareholders of the firm, consistent with the commonly expressed intuition.<sup>26</sup>

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<sup>25</sup>The additional requirement of  $\mathbb{E}[b] < \beta$  in part (i) of Proposition 4 is a sufficient condition that guarantees that the gains from trade of small shareholders, which contribute to  $W^*$ , also increase in  $\beta$ .

<sup>26</sup>Unlike part (i) of Proposition 4, parts (ii.a) and (ii.b) require additional conditions on  $\alpha$ . In particular, requiring  $\alpha > \underline{\alpha}$  in (ii.a) (and a sufficiently small  $\alpha$  in (ii.b)) guarantees that the bias of the median voter

**Divergence among dispersed shareholders.** A positive voting premium emerges in our setting only if the blockholder is able to move the median voter. The next result shows that this can happen only if there is some heterogeneity of preferences among dispersed shareholders.

**Corollary 2** *Suppose that all dispersed shareholders have the same bias  $b$ , which differs from that of the blockholder,  $b \neq \beta$ . Then the voting premium is zero.*

The situation described in Corollary 2 could arise in a setting in which dispersed shareholders have the same valuation of cash flows and the blockholder can reduce these cash flows by diluting the assets of the firm if the proposal is accepted. Then all dispersed shareholders have the same  $b$  and  $b < \beta$ , since the blockholder benefits more from the proposal. This example is discussed in more detail in Section B of the Online Appendix, where we also discuss an example for the opposite case with  $b > \beta$ .

The key point is that in our setting, the blockholder does not acquire majority control. If small shareholders are homogeneous, the median voter is always a small shareholder and the blockholder does not have the ability to change his bias. Hence, heterogeneity among dispersed shareholders is critical for the existence of a positive voting premium in our setting.

#### 5.4.4 Liquidity of voting vs. non-voting shares

Price impact is often used as a measure of liquidity. Liquidity measured in this way is endogenous in our setting because voting rights are bundled with cash flow rights in voting shares. As a consequence, the liquidity of voting shares generally differs from that of non-voting shares. To see this, note from (16) that the total price impact of the blockholder's trade is

$$\frac{dp^*}{dy} = \gamma + \frac{\partial p^*}{\partial(-q^*)} \frac{\partial(-q^*(y))}{\partial y} = \gamma + \underbrace{(\mathbb{E}[b] + q^*) f(q^*)}_{\text{price impact of a vote}} \frac{\partial(-q^*(y))}{\partial y}. \quad (33)$$

The first term,  $\gamma$ , reflects dispersed shareholders' trading costs and would be present even absent voting considerations, e.g., for non-voting shares. The second term reflects the indirect effect through the influence of the blockholder's trades on the median voter,  $-q^*(y)$ , and is pro-  


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increases (decreases) with  $\beta$ . For more details on the role of  $\alpha$  when  $\beta < \underline{\beta}$ , see the discussion of Lemma 4 in the Online Appendix.

portional to the price impact of a vote in equation (29). The sign of the indirect effect depends on whether the resulting change in the median voter benefits or hurts dispersed shareholders.

If the blockholder's and dispersed shareholders' interests are aligned (e.g.,  $-q^*(y^*) < \min\{\beta, \mathbb{E}[b]\}$ ), then the blockholder's trades move the median voter in the direction preferred by both (see Section 5.4.3 for a discussion of two scenarios in which this can occur). This benefits dispersed shareholders and increases the price at which they are willing to supply additional shares; accordingly, the price impact of a vote is positive. Essentially, dispersed shareholders *free-ride* on the blockholder's trades. As a result, the supply function is steeper, the price impact of the blockholder's trades is amplified, and the liquidity of a voting share is smaller compared to a scenario without voting considerations.

By contrast, if the blockholder's and dispersed shareholders' interests are in conflict (e.g.,  $\mathbb{E}[b] < -q^*(y^*) < \beta$ ), then the blockholder's trades move the median voter away from dispersed shareholders. This hurts dispersed shareholders and reduces the reservation price at which they are willing to supply additional shares, so the price impact of a vote (29) is negative. Accordingly, the supply function is flatter, the price impact of the blockholder's trades is attenuated, and the liquidity of a voting share is now greater than that of a non-voting share.

#### 5.4.5 Price impact and the sign of the voting premium

Based on the decomposition of the voting premium in (27), the incentive part of the voting premium is a combination of the marginal benefit of a vote (28) and the price impact of a vote (29). Thus, although the marginal benefit of a vote is always positive, the blockholder only benefits from buying additional shares if his price impact is not too strong. In particular, the voting premium is positive only if moving the median voter increases the value of the blockholder's stake by more than it increases the costs of his trades. This argument has important implications for the sign of the voting premium.

**Conflict and a positive voting premium.** If the blockholder's trades move the median voter in the direction that hurts dispersed shareholders, the voting premium is positive. This is because in this case, a more activist median voter not only increases the value of the blockholder's stake, but also reduces the price he has to pay to dispersed shareholders for a marginal share. Interestingly, this also implies that the voting rights embedded in the shares have op-

posite effects on the *price* of the shares and the *price impact* of trades: the embedded voting rights increase the price of the shares but decrease the price impact of trades.

**Free-riding and a negative voting premium.** If the blockholder's trades move the median voter in the direction that benefits dispersed shareholders, dispersed shareholders free-ride on the blockholder's trades and increase the price at which they are willing to sell shares. As a result, the blockholder's combined incentives to move the median voter, and hence the voting premium, decrease. In general, this does not prevent a positive voting premium. For example, if the blockholder has a positive endowment  $\alpha$  and the trading frictions  $\gamma$  are large (as under the assumptions of Proposition 2), then the voting premium is always non-negative. Intuitively, in this case, the marginal benefit of a vote is sufficiently large because the blockholder's ability to move the median voter in his preferred direction increases the value of his entire post-trade stake  $\alpha + y$ , whereas his price impact only applies to his trade  $y$ . However, if the blockholder has no endowment, then a negative voting premium may arise:

**Proposition 5.** *Suppose  $\alpha = 0$ . There exists  $\bar{\gamma} < \infty$  such that if  $\gamma > \bar{\gamma}$ , then the equilibrium exists and is unique. In equilibrium, the voting premium is negative if and only if  $\mathbb{E}[b] < \beta < \underline{\beta}$ . In this case, the blockholder buys shares ( $y^* > 0$ ) and the share price exhibits a negative voting premium:  $p^* < p_{CF}(q^*(y^*))$  in (25).*

Intuitively, if  $\beta < \underline{\beta}$ , then the blockholder is less activist than the median voter, so the median voter becomes less activist as the blockholder buys shares,  $\frac{\partial(-q^*(y))}{\partial y} < 0$ . Moreover, (27)-(29) continue to hold for  $\alpha = 0$  and imply that the voting premium  $VP(y)$  simplifies to

$$\frac{\partial(-q^*(y))}{\partial y} y \left[ \frac{\partial v(\beta, q^*)}{\partial(-q^*)} - \frac{\partial p^*}{\partial(-q^*)} \right] \frac{\gamma}{2\gamma + \eta} = \frac{\partial(-q^*(y))}{\partial y} y (\beta - \mathbb{E}[b]) f(q^*(y)) \frac{\gamma}{2\gamma + \eta}, \quad (34)$$

which is simply the marginal effect of moving the median voter on the blockholder's net trading profits, and is equal to the difference between the sensitivities of, respectively, the blockholder's and small shareholders' valuations to a change in the median voter. Thus, the blockholder's net marginal payoff from moving the median voter is negative if the average dispersed shareholder is even *less* activist than the blockholder ( $\mathbb{E}[b] < \beta$ ): Then a less activist median voter increases the valuation of the average dispersed shareholder, and thereby the stock price, even more than the valuation of the blockholder.



The scenario in Proposition 5 obtains because the interests of the blockholder and those of dispersed shareholders are aligned, but dispersed shareholders are more extreme and benefit more from the resulting change in the voting outcome. For example, the blockholder may be reluctant to support a certain management proposal, but dispersed shareholders may be more strongly biased against this proposal than the blockholder himself. Then, even though the blockholder values the voting rights per se (the marginal benefit of a vote (28) is positive), his overall incentives to accumulate voting rights become negative. As a result, the blockholder buys fewer shares than if he could buy cash flow rights separately, i.e., if they were not bundled with voting rights. Thus, free-riding by dispersed shareholders results in a negative voting premium if the blockholder has no endowment and cares only about his trading profits.

The negative voting premium is directly related to the differential liquidity of voting and non-voting shares discussed in Section 5.4.4. If the price impact of trading voting shares is much stronger than the price impact of trading non-voting shares (the second term in (33) is large), then the blockholder’s demand for voting shares can be smaller than his demand for non-voting shares, even though he values the voting rights per se. This results in a negative premium on the price of voting shares or, in some sense, an “illiquidity discount” due to the attached voting rights. Moreover, while Propositions 2 and 5 imply that for large  $\gamma$ , a negative voting premium arises only when the blockholder has no initial endowment ( $\alpha = 0$ ), the existence of a negative voting premium is more general: the same intuition implies that if  $\gamma$  is not too large, a negative voting premium can also arise for small but strictly positive  $\alpha$ .

## 6 Dual-class shares

In the baseline model, votes are always bundled with cash flow rights in a fixed proportion. In this section, we introduce a dual-class share structure (e.g., [Zingales \(1995\)](#); [Nenova \(2003\)](#)), which allows investors to build portfolios with different proportions of cash flow to voting rights. Specifically, suppose that in addition to the traded voting shares, investors can also trade non-voting shares. We assume that the blockholder and each dispersed shareholder are endowed with  $\hat{\alpha} \in [0, 1]$  and  $\hat{e} \in [0, 1 - \hat{\alpha}]$  non-voting shares, respectively, so that the total number of outstanding non-voting shares lies in the interval  $[0, 1]$ . Notice that we allow for the supply of non-voting shares to be zero (i.e.,  $\hat{\alpha} = \hat{e} = 0$ ), which could capture the creation of non-voting

securities in derivatives markets. Denote by  $\hat{x}$  and  $\hat{y}$  the trades of dispersed shareholders and the blockholder in the non-voting shares, respectively. The utility of dispersed shareholders is given by

$$\hat{u}(d, \theta, b, x, \hat{x}; \gamma, e, \hat{e}) = (e + x)v(d, \theta, b) - \frac{\gamma}{2}x^2 + (\hat{e} + \hat{x})v(d, \theta, b) - \frac{\gamma}{2}\hat{x}^2. \quad (35)$$

We assume that the parameter for trading costs  $\gamma$  is the same for these two securities, to make sure that the price differential between voting and non-voting shares does not stem from differences in the microstructure of these markets. Similarly, the blockholder's utility is given by  $u(d, \theta, \beta, y, \hat{y}; \eta, \alpha, \hat{\alpha})$ . Notice that in principle, shorting of non-voting shares is feasible. However, we assume that the trading costs  $\gamma$  and  $\eta$  are large enough, so that  $e + x + \hat{e} + \hat{x} > 0$  and  $\alpha + y + \hat{\alpha} + \hat{y} > 0$ , i.e., the net cash flow exposure of each investor is always non-negative.

Suppose first that the decision rule  $q^*$  is exogenous, similar to the hypothetical scenario considered in Section 5. With an exogenous decision rule  $q^*$ , the trading strategies of all investors in each market are given by the expressions in Proposition 2, assuming that  $\frac{\partial(-q^*(y))}{\partial y} = 0$ , and hence,  $MPV = 0$ . Indeed, if the decision rule is not affected by trading, then the existence of the market for non-voting shares does not affect trading in the market for voting shares, and vice versa. This is because investors have no budget constraints and the trading costs apply to each market separately. Moreover, although the endowments of non-voting shares are generally different from the endowments of voting shares, the trading quantities are the same as in the baseline model, since they are invariant to the levels of the endowment. This observation implies that with an exogenous cutoff  $q^*$ , the prices of voting and non-voting shares must be identical. Indeed, given  $(y, \hat{y})$  and  $q^*$ , the difference in prices is

$$p(y, q^*) - p(\hat{y}, q^*) = \gamma y + v(\mathbb{E}[b], q^*) - (\gamma \hat{y} + v(\mathbb{E}[b], q^*)) = \gamma(y - \hat{y}),$$

and since  $y = \hat{y}$ , the two prices are the same.

Next, consider the model where  $q^*$  is determined endogenously by voting. By assumption, the net positions of dispersed shareholders and the blockholder are always non-negative. Therefore, a dispersed shareholder with bias  $b$  votes for the proposal if and only if  $q + b > 0$ , and the blockholder votes for the proposal if and only if  $q + \beta > 0$ . Note also that for a given  $q^*$  and  $(y, \hat{y})$ , the trading strategies of dispersed shareholders in the voting and non-voting shares are

the same as in the baseline model. Thus, the identity of the median voter as a function of the blockholder's trade, namely  $q^*(y)$ , is determined as in the baseline model (see Proposition 1). This implies that given  $y$ , the median voter is unaffected by  $\hat{y}$ , i.e., the trades that take place in the market for non-voting shares. However, the presence of non-voting shares changes the blockholder's trades of voting shares, because he internalizes the effect of the voting outcome on the value of his non-voting shares. The objective of the blockholder becomes:

$$\max_{y, \hat{y}} \Pi(y, \hat{y}) = (\alpha + y) v(\beta, q^*(y)) - yp^*(y) - \frac{\eta}{2} y^2 + (\hat{\alpha} + \hat{y}) v(\beta, q^*(y)) - \hat{y} \hat{p}^*(\hat{y}) - \frac{\eta}{2} \hat{y}^2, \quad (36)$$

and the blockholder's marginal payoff from buying additional voting shares is

$$\frac{d\Pi(y, \hat{y})}{dy} = \underbrace{\frac{\partial \Pi(y, \hat{y})}{\partial y}}_{MPC(y, \hat{y})} + \underbrace{\frac{\partial \Pi(y, \hat{y})}{\partial (-q^*(y))} \frac{\partial (-q^*(y))}{\partial y}}_{MPV(y, \hat{y})}. \quad (37)$$

We obtain the following result:

**Proposition 6 (Dual-class shares)** *If the blockholder and dispersed shareholders can trade in voting and non-voting shares, the voting premium is:*

$$p_{voting}^* - p_{non-voting}^* = \gamma (y^* - \hat{y}^*) = \frac{\gamma}{2\gamma + \eta} MPV(y^*, \hat{y}^*), \quad (38)$$

where

$$MPV(y, \hat{y}) = \frac{\partial (-q^*(y))}{\partial y} \left[ \underbrace{(\alpha + y + \hat{\alpha} + \hat{y}) \frac{\partial v(\beta, q^*(y))}{\partial (-q^*)}}_{\text{marginal benefit of a vote}} - \underbrace{\left( y \frac{\partial p_{voting}^*(y)}{\partial (-q^*)} + \hat{y} \frac{\partial p_{non-voting}^*(y)}{\partial (-q^*)} \right)}_{\text{price impact of a vote}} \right]. \quad (39)$$

Proposition 6 shows that the dual-class voting premium is proportional to  $MPV(y, \hat{y})$ , which is the analog of (26) in the baseline model. Thus, the blockholder's marginal payoff from buying voting rights translates into an actual price difference between voting and non-voting shares. This price differential, and hence the voting premium, is possible only because there are trading frictions and the mass of investors who can demand shares in our model is bounded. Such limits to arbitrage seem necessary for a voting premium to emerge.

Eq. (39) shows that the voting premium can be decomposed into the same components as in the baseline model. Note also that the voting premium depends on  $\hat{y}^*$ , which means that the volume of trades in the market for non-voting shares affects the blockholder’s incentives to buy voting shares, and hence the voting premium. Intuitively, the blockholder’s position in non-voting shares gives him additional incentives to change the median voter and increases his marginal benefit of a vote. The shift in the median voter then changes dispersed shareholders’ valuations and thus the price the blockholder has to pay for non-voting shares.

## 7 Extensions

In this section, we briefly discuss several other implications of the baseline model and its extensions. The complete analysis and explanation of these results is in the Online Appendix.

**Exit and a positive voting premium.** In the context of our baseline model, we show that, although the blockholder has the power to gain influence over the voting outcome by buying additional shares, he may nevertheless choose to do the opposite: sell shares to dispersed shareholders and thereby give up his influence over the voting outcome, while demanding a premium from the dispersed shareholders. Thus, the tension between exit and voice (e.g., [Hirschman \(1970\)](#)) also exists in our model, which demonstrates that the incentives to exit can prevail even when the voting premium is positive. Hence, a positive voting premium does not necessarily indicate a more concentrated ownership structure. This analysis is presented in Section D.1 of the Online Appendix.

**Vote trading.** Our baseline model focuses on the case where one security has voting rights bundled with cash flow rights. In practice, votes can often be traded separately from cash flow rights, for example, through share lending. In Section D.2 of the Online Appendix, we extend the model by adding a second market in which voting rights are traded separately. Since dispersed shareholders are never pivotal for the voting outcome, they are willing to supply their votes for an arbitrarily small price. Hence, the price of a vote is zero in this setting. However, as long as the blockholder’s ability to accumulate voting power through the market for votes is limited, the voting premium can still be strictly positive. Thus, the price of a separately

traded vote is conceptually different from the voting premium for a share that bundles cash flow and voting rights, because small shareholders value cash flow rights and the bundling then gives rise to an upward-sloping supply function.

**Influence premium.** In practice, blockholders can exert influence even without having formal control rights if they can influence the company’s management. In Section D.3 of the Online Appendix, we analyze a version of the model in which decisions are taken by management rather than by voting, and management gives some weight to the value of its current shareholder base, represented by the preferences of the post-trade average shareholder. Then the blockholder’s trades influence decisions by changing these preferences, and the blockholder values this influence, which may give rise to an “influence premium” on the share price. The influence premium is different from the voting premium and can even be larger. In particular, accumulating more shares always increases the blockholder’s influence on management, but it does not always increase the blockholder’s impact if decisions are taken by a shareholder vote.

**Multiple blockholders.** Section D.4 of the Online Appendix generalizes our model to the case with multiple blockholders. It shows that the voting premium declines with the number of blockholders if they share the same preferences. The reasons are the same as in related settings when multiple investors with market power behave like Cournot competitors (Kyle (1989), Edmans and Manso (2011)). In our setting, they free ride on each other’s efforts to move the median voter. In contrast, if the blockholders are sufficiently heterogeneous, their trades pull the median voter in opposite directions. Then, as the blockholders’ biases become more extreme, each blockholder tries harder to gain influence over the voting outcome, which results in a higher voting premium.

**Vote participation** Implicit to our analysis is that dispersed shareholders participate in the vote even though they do not expect to be pivotal for the outcome. In practice, institutional investors vote their shares even if they are unlikely to be pivotal to avoid being accused for breaching their fiduciary duties to their ultimate investors. Retail investors also vote, but at a relatively low rate (?). In general, investors with stronger views about the proposal (i.e., larger  $|b|$ ) are expected to participate and vote with a higher probability. We illustrate how

such selective participation can be incorporated into our analysis in Section D.5 of the Online Appendix. We show that it changes the composition of the voter base, and as a result, the identity of the median voter. Other than that, our analysis can be performed as in the baseline model and generates qualitatively similar results.

## 8 Empirical implications and measures of the voting premium

There is a large empirical literature that provides measures of the voting premium and analyses of the cross-sectional and time-series variation of the voting premium. The purpose of this section is to locate the model developed above in the context of the existing empirical evidence and, conversely, shed some light on the empirical discussion by exploring the implications of our model. Specifically, it is not the purpose of this section to offer a comprehensive survey of empirical studies and methodologies and their potential strengths and shortcomings.<sup>27</sup>

Broadly, there are five major strategies that have been developed in the literature to measure the voting premium and the economic value of voting power. We survey 40 studies in more detail in Table 1 in the Appendix and provide a summary in the table below. Of these studies, 15 use data on the US, 4 on Germany, 3 on Italy, 3 are cross-country studies, and the rest provide evidence on 11 other countries.

Methodology	Avg. (%)	Median (%)	Number of studies
Dual-class shares	23.59	14.53	23
Block-trade premium	41.50	29.55	9
Option replication	0.20	0.16	5
Equity lending	0.01		2
Record-day trading	0.09	0.12	1

<sup>27</sup>Some papers already contain surveys of different strands of this literature. [Rydqvist \(1992\)](#) provides an early survey of studies on dual-class shares and [Dittmann \(2004\)](#), [Adams and Ferreira \(2008\)](#), and [Kind and Poltera \(2013\)](#) provide more recent updates.

The most salient feature of these studies is that they report very divergent estimates of the voting premium. Below, we first discuss why estimates of the voting premium may vary across methodologies (Section 8.1) and then the cross-sectional variation of voting premiums within methodologies (Section 8.2) and relate them to our model.

## 8.1 Differences across methodologies

**Marginal values vs. block values.** Most methods to estimate the voting premium measure the value of a marginal vote. This applies to all methods that rely on stock market prices, i.e., all methods except for the block-trade premium. By contrast, block trades reveal the average valuation of a voting right for the entire block. The table above shows that block trades are associated with significantly larger premiums (average: 41.50%; median: 29.55%) than found in studies of dual-class share premiums (average: 23.59%; median: 14.53%) or those using the three other methods. Based on our model, we would expect the blockholder's willingness to pay for an entire block of shares to be larger than his willingness to pay for an additional voting share. In particular, the equilibrium  $MPV$  in our model may equal zero if the blockholder is the median voter at his equilibrium trading amount  $y^*$  (Proposition 2), resulting in a zero dual-class share premium (Proposition 6, equation (38)). However, his average, per-share willingness to pay for a block of votes of size  $y^*$  may be much larger.

**Voting yields and capitalized voting premiums.** In addition, it is salient from the table that studies relying on dual-class shares and block-trades obtain much larger estimates than the other three methods. We attribute this to the fact that the former two methods capitalize the value of the voting right over longer time horizons, which span potentially infinitely many future shareholder meetings. In contrast, the three other studies estimate the voting yield, which captures a period of one year or less. In the Online Appendix, we calibrate a simple valuation model and show that once the difference in the time horizon is accounted for, the estimates from these two sets of methods are in fact consistent with each other.

**Separate vs. joint trading of cash flow and voting rights.** Another important difference between the methodologies is whether they estimate the price of the vote that is traded separately (as in the equity lending market) or the price of the vote that is traded in con-

junction with cash flow rights (as in the comparison of two classes of stock with differential voting rights). Our analysis emphasizes that the two types of methodologies could give very different estimates of the price of the vote. Indeed, in the extension to a separate market for votes discussed above, we show that the premium on the price of voting shares could be strictly positive even if the price of a separately traded vote is zero.

## 8.2 The cross-sectional variation in the voting premium

This section offers observations on the cross-sectional variation of the voting premium and discusses them in the context of our model.

**Negative values of the voting premium.** One implication from our analysis is that the voting premium can sometimes be negative, which emanates from the free-rider effect and the possibly substantial price impact of the blockholder’s trades (see Proposition 5 and the related discussion). Interestingly, while the estimates of the mean and median of the voting premium in the studies surveyed in Table 1 are always positive, many studies report that the voting premium is negative for some companies.<sup>28</sup> These findings are consistent with our model, but are difficult to interpret in the context of extant theories. Empirical studies often explain them by pointing out that voting shares may suffer from a liquidity discount relative to non-voting shares. This explanation is in line with our argument: the negative voting premium in our model arises exactly because the trading of voting shares has a stronger price impact than the trading of non-voting shares. If we define liquidity as price impact, then our model predicts the differential liquidity of voting and non-voting shares, which arises because the blockholder’s accumulation of voting rights changes dispersed shareholders’ valuations.

**Voting premiums, takeovers, and shareholder meetings.** One of the standard explanations for how the blockholder’s willingness to pay a premium for voting control is translated into higher prices for voting shares is the takeover mechanism, and several empirical studies find support for this explanation.<sup>29</sup> However, this theory has some limitations. First, since

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<sup>28</sup>E.g., see [Rydqvist \(1996\)](#), [Nenova \(2003\)](#), and [Caprio and Croci \(2008\)](#) for the dual-class share premium and [Albuquerque and Schroth \(2010\)](#) and [Albuquerque and Schroth \(2015\)](#) for the block trading premium.

<sup>29</sup>See Section 2 for details on these theories. For empirical evidence see [Bergström and Rydqvist \(1992\)](#); [Zingales \(1995\)](#); [Rydqvist \(1996\)](#); and [Smith and Amoako-Adu \(1995\)](#).



the 1990s, many countries have enacted coattail provisions, which mandate equal treatment of all classes of shares in control changes (Maynes (1996); Nenova (2003)). Second, Dittmann (2004) surveys 12 studies of companies with dual-class share structures and shows that if investors would correctly anticipate the ex-post frequencies of takeovers and takeover premiums paid, then the premium on voting shares in dual-class firms should be smaller by about one order of magnitude compared to the observed premium in most countries. Hence, the takeover explanation is probably only a partial explanation of premiums on voting shares.

Differently from this argument, our analysis shows how the voting premium can arise without contests for majority control, and solely as a result of blockholders' desire to influence the voting outcomes at shareholder meetings. This prediction is consistent with the findings of the more recent literature, which analyzes the time-series variation in the voting premium and finds that the voting premium is largest around shareholder meetings compared to other periods of the year (see Kind and Poltera (2013); Kalay, Karakas, and Pant (2014); Kind and Poltera (2017); Fos and Holderness (2020)).

**Voting premiums and ownership structure.** Studies on the relationship between the voting premium and ownership concentration show that it is often non-monotonic: the value of voting rights is small both if ownership is very dispersed and if it is very concentrated with one blockholder who has majority control (Kind and Poltera (2013)). Therefore, one common methodology uses the probability of being pivotal inferred from oceanic Shapley values instead of ownership concentration to predict the voting premium.<sup>30</sup> Our analysis in Section D.4 of the Online Appendix suggests a new empirical direction by showing that it is not only the concentration of ownership and the probability of being pivotal that matter, but also the preferences of blockholders. Specifically, if blockholders have similar preferences, then ownership concentration is positively correlated with the voting premium, and if blockholders disagree with each other, the voting premium increases the more they disagree.

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<sup>30</sup>See Section 2 for the discussion of a theoretical model by Rydqvist (1987), which uses oceanic Shapley values to explain dual-class share premiums. Based on this model, Rydqvist (1987) derives an empirical measure of relative voting power, which is widely used (e.g., Zingales (1994), Zingales (1995), Chung and Kim (1999), Caprio and Croci (2008), and Nenova (2003)).

## 9 Conclusion

We develop a theory of voting and trading in which a blockholder and dispersed shareholders trade with each other and then vote on a proposal. We analyze trading decisions and the emergence of a premium for voting shares, which results from the interplay of two forces: the blockholder's willingness to purchase shares in order to affect the preferences of the median voter; and dispersed shareholders' reservation prices, which depend on the median voter, thus giving rise to an upward-sloping supply function of shares to the blockholder.

Since the voting premium depends on the blockholder's willingness to pay for a marginal voting share, it reflects neither his voting power nor the overall value of a voting block to him. It is also not monotonically related to the degree of conflict between the blockholder and small shareholders and thus, probably not a good measure for such a conflict. However, the alignment of the blockholder's preferences with those of small shareholders tends to increase the blockholder's price impact and make voting shares less liquid. In extreme cases, this may result in a negative voting premium, when blockholders limit their purchases to prevent dispersed shareholders from free-riding on their accumulation of shares.

Based on our theory, we suggest that future empirical analyses of the voting premium distinguish between measures based on the average and the marginal value of a vote, as well as between measures based on votes bundled with and without cash flow rights. Empirical studies should also pay careful attention to the heterogeneity of the shareholder base in terms of shareholders' size and preferences, and recognize that large blockholders will often have neither the ability nor the incentives to affect voting outcomes through trading, resulting in negligible voting premiums.

## References

- Adams, Renee B. and Daniel Ferreira. 2008. “One Share, One Vote: The Empirical Evidence.” *Review of Finance* 12 (1):51–91.
- Admati, Anat R. and Paul C. Pfleiderer. 2009. “The ‘Wall Street Walk’ and Shareholder Activism: Exit as a Form of Voice.” *Review of Financial Studies* 22 (7):2445–2485.
- Admati, Anat R., Paul C. Pfleiderer, and Josef Zechner. 1994. “Large shareholder activism, risk sharing, and financial market equilibrium.” *Journal of Political Economy* 102 (6):1097–1130.
- Aggarwal, Reena, Pedro A. C. Saffi, and Jason Sturgess. 2015. “The Role of Institutional Investors in Voting: Evidence from the Securities Lending Market.” *The Journal of Finance* 70 (5):2309–2346.
- Albuquerque, Rui A. and Enrique Schroth. 2010. “Quantifying private benefits of control from a structural model of block trades.” *Journal of Financial Economics* 96 (1):33–55.
- . 2015. “The Value of Control and the Costs of Illiquidity.” *Journal of Finance* 70 (4):1405–1455.
- Austen-Smith, David and Jeffrey S. Banks. 1996. “Information Aggregation, Rationality, and the Condorcet Jury Theorem.” *American Political Science Review* 90 (1):34–45.
- Bar-Isaac, Heski and Joel D. Shapiro. 2020. “Blockholder Voting.” *Journal of Financial Economics* 136 (3):695–717.
- Barak, Ronen and Beni Lauterbach. 2011. “Estimating the private benefits of control from partial control transfers: methodology and evidence.” *International Journal of Corporate Governance* 2 (3/4):183–200.
- Barclay, Michael J. and Clifford G. Holderness. 1989. “Private benefits from control of public corporations.” *Journal of Financial Economics* 25 (2):371–395.
- Baron, David P. and John A. Ferejohn. 1989. “Bargaining in Legislatures.” *American Political Science Review* 83 (4):1181–1206.
- Bergström, Clas and Kristian Rydqvist. 1992. “Differentiated Bids for Voting and Restricted Voting Shares in Public Tender Offers.” *Journal of Banking and Finance* 16:97–114.
- Bigelli, Marco and Ettore Croci. 2013. “Dividend privileges and the value of voting rights: Evidence from Italy.” *Journal of Empirical Finance* 24:94–107.
- Blair, Douglas H., Devra L. Golbe, and James M. Gerard. 1989. “Unbundling the Voting Rights and Profit Claims of Common Shares.” *Journal of Political Economy* 97 (2):420–443.
- Bolton, Patrick, Tao Li, Enrichetta Ravina, and Howard Rosenthal. 2020. “Investor ideology.” *Journal of Financial Economics* 137 (2):320–352.
- Bolton, Patrick and Ernst-Ludwig von Thadden. 1998. “Blocks, Liquidity, and Corporate Control.” *The Journal of Finance* 53 (1):1–25.

- Bradley, Michael. 1980. “Interfirm Tender Offers and the Market for Corporate Control.” *Journal of Business* 53 (4):345–376.
- Brav, Alon and Richmond D. Mathews. 2011. “Empty Voting and the Efficiency of Corporate Governance.” *Journal of Financial Economics* 99 (2):289–307.
- Broussard, John Paul and Mika Vaihekoski. 2019. “Time-Variation of Dual-Class Premia.” *Working Paper, Rutgers School of Business* .
- Bubb, Ryan and Emiliano Catan. 2021. “The Party Structure of Mutual Funds.” *Review of Financial Studies (forthcoming)* .
- Burkart, Mike, Denis Gromb, and Fausto Panunzi. 1998. “Why Higher Takeover Premia Protect Minority Shareholders.” *Journal of Political Economy* 106 (1):172–204.
- Burkart, Mike and Samuel Lee. 2008. “The One Share - One Vote Debate: A Theoretical Perspective.” *Review of Finance* 12 (1):1–49.
- . 2010. “Signaling in Tender Offer Games.” *CEPR Discussion Paper (DP7938)*.
- Bushee, Brian J. 1998. “The Influence of Institutional Investors on Myopic R&D Investment Behavior.” *The Accounting Review* 73 (3):305–333.
- Caprio, Lorenzo and Ettore Croci. 2008. “The determinants of the voting premium in Italy: The evidence from 1974 to 2003.” *Journal of Banking & Finance* 32 (11):2433–2443.
- Casella, Alessandra, Aniol Llorente-Saguer, and Thomas R. Palfrey. 2012. “Competitive Equilibrium in Markets for Votes.” *Journal of Political Economy* 120 (4):593–658.
- Christoffersen, Susan E. K., Christopher Geczy, David K. Musto, and Adam V. Reed. 2007. “Vote Trading and Information Aggregation.” *Journal of Finance* 62 (6):2897–2929.
- Chung, Kee H. and Jeong-Kuk Kim. 1999. “Corporate ownership and the value of a vote in an emerging market.” *Journal of Corporate Finance* 5 (1):35–54.
- Cox, Steven R. and Dianne M. Roden. 2002. “The source of value of voting rights and related dividend promises.” *Journal of Corporate Finance* 8 (4):337–351.
- Cvijanovic, Dragana, Amil Dasgupta, and Konstantinos E. Zachariadis. 2016. “Ties That Bind: How Business Connections Affect Mutual Fund Activism.” *Journal of Finance* 71 (6):2933–2966.
- Cvijanovic, Dragana, Moqi Groen-Xu, and Konstantinos E. Zachariadis. 2020. “Free-Riders and Underdogs: Participation in Corporate Voting.” *ECGI - Finance Working Paper (649/2020)*.
- Dasgupta, Amil, Vyacheslav Fos, and Zacharias Sautner. 2020. “Institutional Investors and Corporate Governance.” *Working Paper, London School of Economics* .
- Daske, Stefan and Olaf Ehrhardt. 2002. “Kursunterschiede und Renditen deutscher Stamm- und Vorzugsaktien.” *Financial Markets and Portfolio Management* 16 (2):179–207.

- DeAngelo, Harry and Linda DeAngelo. 1985. “Managerial Ownership of Voting Rights - A Study of Public Corporations with Dual Classes of Common Stock.” *Journal of Financial Economics* 14 (1):33–69.
- Dekel, Eddie and Asher Wolinsky. 2012. “Buying shares and/or votes for corporate control.” *The Review of Economic Studies* 79 (1):196–226.
- DeMarzo, Peter. 1993. “Majority Voting and Corporate Control: The Rule of the Dominant Shareholder.” *Review of Economic Studies* 60 (204):713–734.
- Desai, Mihir A. and Li Jin. 2011. “Institutional tax clienteles and payout policy.” *Journal of Financial Economics* 100 (1):68–84.
- Dhillon, Amrita and Silvia Rossetto. 2015. “Ownership Structure, Voting, and Risk.” *Review of Financial Studies* 28 (2):521–560.
- Dittmann, Ingolf. 2003. “Measuring Private Benefits of Control from the Returns of Voting and Non-Voting Shares.” *Working Paper, Erasmus University* .
- . 2004. “Block Trading, Ownership Structure, and the Value of Corporate Votes.” *Working Paper, Erasmus University* .
- Drèze, Jacques H. 1985. “(Uncertainty and) The Firm in General Equilibrium Theory.” *The Economic Journal* 95:1–20.
- Dyck, I. J. Alexander and Luigi Zingales. 2004. “Private benefits of control: An international comparison.” *Journal of Finance* 59 (2):537–600.
- Edmans, Alex. 2009. “Blockholder Trading, Market Efficiency, and Managerial Myopia.” *Journal of Finance* 64 (6):2481–2513.
- . 2014. “Blockholders and Corporate Governance.” *Annual Review of Financial Economics* 6 (1):23–50.
- Edmans, Alex and Clifford G. Holderness. 2017. *Chapter 8 - Blockholders: A Survey of Theory and Evidence*. in: Benjamin E. Hermalin and Michael S. Weisbach, *The Handbook of the Economics of Corporate Governance*, North-Holland, 541–636.
- Edmans, Alex and Gustavo Manso. 2011. “Governance Through Trading and Intervention: A Theory of Multiple Blockholders.” *Review of Financial Studies* 24 (7):2395–2428.
- Esö, Peter, Stephen Hansen, and Lucy White. 2014. “A Theory of Vote-trading and Information Aggregation.” *Working Paper, University of Oxford*.
- Fama, Eugene F. and Kenneth R. French. 2002. “The Equity Premium.” *Journal of Finance* 57 (2):637–660.
- Feddersen, Timothy J. and Wolfgang Pesendorfer. 1996. “The Swing Voter’s Curse.” *American Economic Review* 86 (3):408–424.
- Fos, Vyacheslav and Clifford G. Holderness. 2020. “The Price of a Marginal Vote: What Happens when Stocks Go Ex Vote.” *Working Paper, Boston College* .

- Franks, Julian and Colin Mayer. 2001. “Ownership and Control of German Corporations.” *Review of Financial Studies* 14 (4):943–977.
- Gardiol, Lucien, Rajna Gibson-Asner, and Nils S. Tuchschnid. 1997. “Are liquidity and corporate control priced by shareholders? Empirical evidence from Swiss dual class shares.” *Journal of Corporate Finance* 3 (4):299–323.
- Gaspar, José-Miguel, Massimo Massa, and Pedro Matos. 2005. “Shareholder Investment Horizons and the Market for Corporate Control.” *Journal of Financial Economics* 76 (1):135–165.
- Gevers, Louis. 1974. *Competitive Equilibrium of the Stock Exchange and Pareto Efficiency*. London: in: Jacques H. Drèze, Allocation under Uncertainty: Equilibrium and Optimality, Proceedings from a workshop sponsored by the International Economic Association, Palgrave Macmillan (UK), 167–191.
- Goetzmann, William N., Andrey Ukhov, and Matthew I. Spiegel. 2002. “Modeling and Measuring Russian Corporate Governance: The Case of Russian Preferred and Common Shares (English Version).” *Working Paper, Yale School of Management* .
- Grossman, Sanford J. and Oliver D. Hart. 1980. “Takeover Bids, The Free Rider Problem, and the Theory of the Corporation.” *Bell Journal of Economics* 11:42–64.
- . 1988. “One Share-One Vote and the Market for Corporate Control.” *Journal of Financial Economics* 20:175–202.
- Gurun, Umit and Oguzhan Karakas. 2020. “Earnings and the Value of Voting Rights.” *Working Paper, University of Texas at Dallas* .
- Harris, Milton and Artur Raviv. 1988. “Corporate Governance: Voting Rights and Majority Rules.” *Journal of Financial Economics* 20:203–236.
- Hayden, Grant M and Matthew T Bodie. 2008. “One Share, One Vote and the False Promise of Shareholder Homogeneity.” *Cardozo Law Review* 30:445–505.
- He, Jie, Jiekun Huang, and Shan Zhao. 2019. “Internalizing Governance Externalities: The Role of Institutional Cross-Ownership.” *Journal of Financial Economics* 134 (2):400–418.
- Hirschman, Albert O. 1970. *Exit, voice, and loyalty: Responses to decline in firms, organizations, and states*, vol. 25. Harvard university press.
- Hoffman-Burchardi, Ulrike. 1999. “Corporate governance rules and the value of control - A study of German dual-class shares.” *FMG Discussion Paper* (315).
- Horner, Melchior R. 1988. “The Value of the Corporate Voting Right: Evidence from Switzerland.” *Journal of Banking and Finance* 12:69–83.
- Hu, Henry T. C. and Bernard Black. 2007. “Hedge Funds, Insiders, and the Decoupling of Economic and Voting Ownership: Empty Voting and Hidden (Morphable) Ownership.” *Journal of Corporate Finance* 13:3443–367.
- Hu, Henry T. C. and Bernard S. Black. 2015. *Debt, Equity and Hybrid Decoupling: Governance and Systemic Risk Implications*. Oxford: Oxford University Press, 349–399.

- Jang, In Ji, Hwagyun Kim, and Mahdi Mohseni. 2019. “What Does the Value of Corporate Votes Tell Us About Future Stock Returns?” *Working Paper, Bentley University* .
- Kahn, Charles and Andrew Winton. 1998. “Ownership Structure, Speculation, and Shareholder Intervention.” *Journal of Finance* 53 (1):99–129.
- Kalay, Avner, Oguzhan Karakas, and Shagun Pant. 2014. “The Market Value of Corporate Votes: Theory and Evidence from Option Prices.” *Journal of Finance* (3):1235–1271.
- Kalay, Avner and Shagun Pant. 2010. “Time Varying Voting Rights and the Private Benefits of Control.” *Working Paper, Tel Aviv University* Tel Aviv University.
- Kelsey, David and Frank Milne. 1996. “The Existence of Equilibrium in Incomplete Markets and the Objective Function of the Firm.” *Journal of Mathematical Economics* 25 (2):229–245.
- Kind, Axel and Marco Poltera. 2013. “The value of corporate voting rights embedded in option prices.” *Journal of Corporate Finance* 22:16–34.
- . 2017. “Shareholder proposals as governance mechanism: Insights from the market value of corporate voting rights.” .
- Kunz, Roger M. and James J. Angel. 1996. “Factors Affecting the Value of the Stock Voting right: Evidence from the Swiss Equity Market.” *Financial Management* 25:7–20.
- Kyle, Albert S. 1989. “Informed Speculation with Imperfect Competition.” *Review of Economic Studies* 56 (3):317–356.
- La Porta, Rafael, Florencio Lopez-de Silanes, Andrei Shleifer, and Robert Vishny. 1999. “Corporate Ownership Around the World.” *Journal of Finance* 54 (2):471–517.
- Lease, Ronald C., John J. McConnell, and Wayne H. Mikkelson. 1983. “The market value of control in publicly-traded corporations.” *Journal of Financial Economics* 11 (1):439–471.
- Levit, Doron and Nadya Malenko. 2011. “Nonbinding Voting for Shareholder Proposals.” *Journal of Finance* 66 (5):1579–1614.
- Levit, Doron, Nadya Malenko, and Ernst Maug. 2020. “Trading and Shareholder Democracy.” *ECGI Finance Working Paper* (631).
- Levy, Haim. 1983. “Economic Evaluation of Voting Power of Common Stock.” *Journal of Finance* 38 (1):79–93.
- Malenko, Andrey and Nadya Malenko. 2019. “Proxy Advisory Firms: The Economics of Selling Information to Voters.” *Journal of Finance* 74 (5):2441–2490.
- Maug, Ernst. 1998. “Large Shareholders as Monitors: Is there a trade-off between liquidity and control?” *Journal of Finance* 53 (1):65–98.
- Maug, Ernst and Kristian Rydqvist. 2009. “Do Shareholders Vote Strategically? Voting Behavior, Proposal Screening, and Majority Rules.” *Review of Finance* 13 (1):47–79.

- Maynes, Elizabeth. 1996. "Takeover rights and the value of restricted shares." *Journal of Financial Research*, 19 (2):157–173.
- McCahery, Joseph A, Zacharias Sautner, and Laura T Starks. 2016. "Behind the scenes: The corporate governance preferences of institutional investors." *Journal of Finance* 71 (6):2905–2932.
- Meggison, William L. 1990. "Restricted Voting Stock, Acquisition Premiums, and the Market Value for Corporate Control." *Financial Review* 25:175–198.
- Meirowitz, Adam and Shaoting Pi. 2021. "The Shareholder's Dilemma: Voting and Trading." *Working Paper*, University of Utah.
- Milnor, J. W. and L. S. Shapley. 1978. "Values of Large Games II: Oceanic Games." 3 (4):290–307.
- Muravyev, Alexander. 2004. "The puzzle of dual class stock in Russia: Explaining the price differential between common and preferred shares." *MPRA Paper* (27726).
- Muus, Christian. 1998. "Non-voting shares in France: an empirical analysis of the voting premium." *Johann Wolfgang Goethe-Universität Frankfurt am Main Working Paper Series: Finance & Accounting* (22).
- Neeman, Zvika and Gerhard O. Orosel. 2006. "On the Efficiency of Vote Buying when Voters Have Common Interests." *International Review of Law and Economics* 26 (4):536–556.
- Nenova, Tatiana. 2003. "The value of corporate votes and control benefits: A cross-country analysis." *Journal of Financial Economics* 68 (3):325–351.
- Neumann, Robert. 2003. "Price Differentials between Dual-class Stocks: Voting Premium or Liquidity Discount?" *European Financial Management* 9 (3):315 – 332.
- Odegaard, Bernt Arne. 2007. "Price differences between equity classes. Corporate control, foreign ownership or liquidity?" *Journal of Banking & Finance* 31 (12):3621–3645.
- Rydqvist, Kristian. 1987. *The Pricing of Shares with Different Voting Power and the Theory of Oceanic Games*. Stockholm School of Economics, 1st ed. ed.
- . 1992. "Dual-Class Shares: A Review." *Oxford Review of Economic Policy* 8:45–57.
- . 1996. "Takeover Bids and the Relative Prices of Shares That Differ in Their Voting Rights." *Journal of Banking and Finance* 20 (8):1407–25.
- Smith, Brian F. and Ben Amoako-Adu. 1995. "Relative Prices of Dual Class Shares." *Journal of Financial and Quantitative Analysis* 30 (2):223–239.
- Speit, Andre and Paul Voss. 2020. "Shareholder Votes on Sale." *Working Paper*, University of Bonn.
- Stulz, René M. 1988. "Managerial Control of Voting Rights - Financing Policies and the Market for Corporate Control." *Journal of Financial Economics* 20:25–54.



- Van Wesep, Edward D. 2014. “The Idealized Electoral College Voting Mechanism and Shareholder Power.” *Journal of Financial Economics* 113 (2):90–108.
- Vinaimont, Tom and Piet Sercu. 2003. “Deviations from ‘One Share, One Vote’ Can Be Optimal: An Entrepreneur’s Point of View.” *Working Paper, Nazarbayev University Graduate School of Business* .
- Zingales, Luigi. 1994. “The Value of the Voting Right: A Study of the Milan Stock Exchange Experience.” *Review of Financial Studies* 7 (1):125–148.
- . 1995. “What Determines the Value of Corporate Votes?” *Quarterly Journal of Economics* 110:1047–1073.

## Appendix - Proofs

**Proof of Lemma 1.** Given the realization of  $q$ , a shareholder with bias  $b$  votes for the proposal if and only if  $q > -b$ . Denote the fraction of post-trade shares voted to approve the proposal by  $\Lambda(q)$ , and note that  $\Lambda(q)$  is weakly increasing. There are three cases. If  $\Lambda(\Delta) \leq \tau$  for the highest possible  $q = \Delta$ , then  $q^*$  in the statement of the lemma is equal to  $\Delta$ . If  $\Lambda(-\Delta) > \tau$  for the lowest possible  $q = -\Delta$ , then  $q^*$  in the statement of the lemma is equal to  $-\Delta$ . Finally, if  $\Lambda(-\Delta) \leq \tau < \Lambda(\Delta)$ , there exists  $q^* \in [-\Delta, \Delta)$  such that the fraction of votes in favor of the proposal is greater than  $\tau$  if and only if  $q > q^*$ , so the proposal is approved if and only if  $q > q^*$ . ■

**Proof of Proposition 1.** Recall that  $\underline{q} = s^{-1}(\tau - \alpha - y; y, q_e^*)$  and  $\bar{q} = s^{-1}(\tau; y, q_e^*)$ , and denote the corresponding functions by  $\underline{q}(y, q_e^*)$  and  $\bar{q}(y, q_e^*)$ . As follows from the arguments in the main text prior to the proposition, the proposal is approved if and only if  $q > -b_{MV}(\beta, y, q_e^*)$ , where

$$b_{MV}(\beta, y, q_e^*) = \begin{cases} -\bar{q}(y, q_e^*) & \text{if } \beta < -\bar{q}(y, q_e^*) \\ \beta & \text{if } -\bar{q}(y, q_e^*) \leq \beta \leq -\underline{q}(y, q_e^*) \\ -\underline{q}(y, q_e^*) & \text{if } -\underline{q}(y, q_e^*) < \beta \end{cases} \quad (40)$$

is the bias of the median voter.

Since shareholders' expectations  $q_e^*$  at the trading stage have to be consistent with the actual decision rule at the voting stage, the equilibrium at the voting stage can be characterized as follows: the proposal is approved if and only if  $q > q^*(y)$ , where

$$-q^*(y) = \begin{cases} \beta_L(y) & \text{if } \beta < \beta_L(y) \\ \beta & \text{if } \beta_L(y) \leq \beta \leq \beta_H(y) \\ \beta_H(y) & \text{if } \beta_H(y) < \beta \end{cases} \quad (41)$$

is the bias of the median voter,  $\beta_L(y)$  and  $\beta_H(y)$  are the solutions of

$$\beta_L(y) = -\bar{q}(y, -\beta_L) \Leftrightarrow s(-\beta_L; y, -\beta_L) = \tau, \quad (42)$$

$$\beta_H(y) = -\underline{q}(y, -\beta_H) \Leftrightarrow s(-\beta_H; y, -\beta_H) = \tau - \alpha - y. \quad (43)$$

Using (13), conditions (42) and (43) can be rewritten as

$$R(\beta_L; y, -\beta_L) = 1 - \frac{\tau}{1 - \alpha - y}, \quad (44)$$

$$R(\beta_H; y, -\beta_H) = 1 - \frac{\tau - \alpha - y}{1 - \alpha - y}. \quad (45)$$

From (12),  $R(b'; y, q^*)$  is a cdf, lies in the unit interval, and

$$\lim_{\beta \rightarrow -\bar{b}} R(\beta; y, -\beta) = 0 \text{ and } \lim_{\beta \rightarrow \bar{b}} R(\beta; y, -\beta) = 1. \quad (46)$$

Hence, solutions to (44) and (45), and therefore, of (42) and (43), exist. Using (12) and

simplifying, we can show that the derivative of  $R(\beta; y, -\beta)$  with respect to  $\beta$  is:

$$\begin{aligned} \frac{\partial R(\beta; y, -\beta)}{\partial \beta} &= g(\beta) \left( 1 + \frac{\beta - \mathbb{E}[b]}{\gamma} \frac{H(-\beta)}{1 - \alpha - y} \right) \\ &\quad - G(\beta) \frac{f(-\beta)}{1 - \alpha - y} \frac{\mathbb{E}[b] - \mathbb{E}[b|b < \beta]}{\gamma}. \end{aligned} \quad (47)$$

From (10) and (11), the first line of (47) equals  $r(\beta; y, -\beta) > 0$ . Since,  $\mathbb{E}[b] > \mathbb{E}[b|b < \beta]$ , the second line is negative. Hence,  $R(\beta; y, -\beta)$  may be non-monotonic in  $\beta$ . From (47),  $\frac{\partial R(\beta; y, -\beta)}{\partial \beta} > 0$  if and only if

$$\frac{\frac{G(\beta)}{g(\beta)} f(-\beta) (\mathbb{E}[b] - \mathbb{E}[b|b < \beta]) + H(-\beta) (\mathbb{E}[b] - \beta)}{1 - \alpha - y} < \gamma,$$

and thus, there exists  $\bar{\gamma} < \infty$  such that if  $\gamma > \bar{\gamma}$ , then  $\frac{\partial R(\beta; y, -\beta)}{\partial \beta} > 0$  for all  $y \geq -\alpha$ . In this case, (46) implies that the solutions to (42)-(43) exist and are unique.

Suppose  $\gamma > \bar{\gamma}$ , such that  $\beta_L(y)$  and  $\beta_H(y)$  are unique. For  $y = -\alpha$  (when the blockholder sells his entire endowment), the right hand sides of (44) and (45) are identical, so we can define

$$\beta^* \equiv \beta_H(-\alpha) = \beta_L(-\alpha), \quad (48)$$

or equivalently,  $R(\beta^*; y, -\beta^*) = 1 - \tau$ . Lemma 2 below shows that  $\beta_L(y)$  is decreasing,  $\lim_{y \nearrow 1 - \tau - \alpha} \beta_L(y) = -\bar{b}$ ,  $\beta_H(y)$  is increasing, and  $\lim_{y \nearrow \tau - \alpha} \beta_H(y) = \bar{b}$ . Using these properties, there are two cases to consider:

1. Suppose  $\beta \in (\beta^*, \bar{b})$ . Then  $\beta > \beta_L(y)$  for all  $y$ , and there exists  $y_H$  such that  $\beta_H(y) \geq \beta$  if and only if  $y \geq y_H$ , where from (45),

$$y_H = 1 - \alpha - \frac{1 - \tau}{G(\beta)} - \frac{1}{\gamma} (\mathbb{E}[b] - \mathbb{E}[b|b < \beta]) H(-\beta). \quad (49)$$

Then, (41) implies that if  $y \geq y_H$ , the median voter is the blockholder (i.e.,  $-q^*(y) = \beta$ ), and if  $y < y_H$ , the median voter is a dispersed shareholder with bias  $\beta_H(y)$ . Suppose  $y < y_H$ . Since  $\beta_H(y)$  is increasing in  $y$  and  $\beta > \beta_H(y)$ , then  $|\beta + q^*(y)| = \beta - \beta_H(y)$  decreases in  $y$ .

2. Suppose  $\beta \in (-\bar{b}, \beta^*)$ . Then  $\beta < \beta_H(y)$  for all  $y$ , and there exists  $y_L$  such that  $\beta_L(y) > \beta$  if and only if  $y < y_L$ , where from (44),

$$y_L = 1 - \alpha - \frac{\tau}{1 - G(\beta)} + \frac{1}{\gamma} \frac{G(\beta)}{1 - G(\beta)} (\mathbb{E}[b] - \mathbb{E}[b|b < \beta]) H(-\beta). \quad (50)$$

Then, (41) implies that if  $y \geq y_L$ , the median voter is the blockholder (i.e.,  $-q^*(y) = \beta$ ), and if  $y < y_L$ , the median voter is a dispersed shareholder with bias  $\beta_L(y)$ . Suppose  $y < y_L$ . Since  $\beta_L(y)$  is decreasing in  $y$  and  $\beta < \beta_L(y)$ , then  $|\beta + q^*(y)| = \beta_L(y) - \beta$  decreases in  $y$ .

Setting  $\bar{y}$  as  $y_H$  if  $\beta \in (\beta^*, \bar{b})$  and as  $y_L$  if  $\beta \in (-\bar{b}, \beta^*)$  completes the proof. Section C.2 in the Online Appendix visualizes the functions  $\beta_L(y)$  and  $\beta_H(y)$ . ■

The next auxiliary lemma is used in the proofs of the baseline model's main results. Its proof is given in Section C of the Online Appendix.

**Lemma 2 (Properties of the median voter)** *Suppose that  $\gamma > \bar{\gamma}$  from the proof of Proposition 1, so that  $\frac{\partial R(\beta; y, -\beta)}{\partial \beta} > 0$  for all  $y \geq -\alpha$  and the solutions  $\beta_L(y)$  and  $\beta_H(y)$  of (42) and (43) are unique for all  $y$ . Then:*

- (i)  $\beta_L(y)$  is decreasing in  $y$  and  $\lim_{y \nearrow 1-\tau-\alpha} \beta_L(y) = -\bar{b}$ .
- (ii)  $\beta_H(y)$  is increasing in  $y$  and  $\lim_{y \nearrow \tau-\alpha} \beta_H(y) = \bar{b}$ .
- (iii) In the limit as  $\gamma \rightarrow \infty$ ,

$$\lim_{\gamma \rightarrow \infty} \beta_L(y) = G^{-1} \left( 1 - \frac{\tau}{1 - \alpha - y} \right), \quad \lim_{\gamma \rightarrow \infty} \beta_H(y) = G^{-1} \left( \frac{1 - \tau}{1 - \alpha - y} \right), \quad (51)$$

and

$$\lim_{\gamma \rightarrow \infty} \frac{\partial \beta_L(y)}{\partial y} = - \frac{1 - G(\lim_{\gamma \rightarrow \infty} \beta_L(y))}{g(\lim_{\gamma \rightarrow \infty} \beta_L(y))(1 - \alpha - y)}, \quad (52)$$

$$\lim_{\gamma \rightarrow \infty} \frac{\partial \beta_H(y)}{\partial y} = \frac{G(\lim_{\gamma \rightarrow \infty} \beta_H(y))}{g(\lim_{\gamma \rightarrow \infty} \beta_H(y))(1 - \alpha - y)}, \quad (53)$$

$$\lim_{\gamma \rightarrow \infty} \beta^* = G^{-1}(1 - \tau). \quad (54)$$

where  $\beta^*$  is given by (48).

**Proof of Proposition 2.** By assumption, the blockholder's trade in equilibrium is  $y \in (-\alpha, 1 - \alpha)$ . Given (4) and (9), we can write

$$\begin{aligned} \Pi(y) &= (\alpha + y)v(\beta, q^*(y)) - yp^*(y) - 0.5\eta y^2 \\ &= \alpha v(\beta, q^*(y)) + y(\beta - \mathbb{E}[b])H(q^*) - (\gamma + 0.5\eta)y^2 \\ &= \alpha v_0 + \alpha \mathbb{E}[\theta|q > q^*(y)]H(q^*) + ((\alpha + y)\beta - yE[b])H(q^*) - (\gamma + 0.5\eta)y^2, \end{aligned}$$

and derive

$$\frac{\partial \Pi(y)}{\partial y} = (\beta - \mathbb{E}[b])H(q^*(y)) - (2\gamma + \eta)y + \frac{\partial(-q^*(y))}{\partial y} [\alpha(q^*(y) + \beta) + y(\beta - \mathbb{E}[b])]f(q^*(y)),$$

where  $q^*(y)$  is given by (41). Both  $\frac{\partial(-q^*(y))}{\partial y}$  and  $\frac{\partial \Pi(y)}{\partial y}$  do not exist when  $\beta = \beta_L(y)$  or  $\beta = \beta_H(y)$ , which correspond to values  $y_L$  and  $y_H$  in Figure A1 in the Online Appendix. In those cases, we interpret  $\frac{\partial(-q^*(y))}{\partial y}$  as the right derivative, which is zero, and  $\frac{\partial \Pi(y)}{\partial y}$  as the right derivative, which is equal  $MPC(y)$ .

We start by giving sufficient conditions under which  $\Pi(y)$  is continuous, concave, and has a unique maximizer. From Proposition 1, there exists a  $\bar{\gamma}_1$  such that, if  $\gamma > \bar{\gamma}_1$ , then  $\beta_L(y)$

and  $\beta_H(y)$  are well defined continuous functions of  $y$ . If so,  $\Pi(y)$  is a continuous function of  $y$  as well. In addition, Lemma 3 in Section C of the Online Appendix shows that there exists  $\bar{\gamma}_2 < \infty$  such that if  $\gamma > \bar{\gamma}_2$ , then  $\Pi(y)$  is a concave function. Combined, if  $\gamma > \max\{\bar{\gamma}_1, \bar{\gamma}_2\}$ , then  $\Pi(y)$  is a continuous and concave function, and hence, it has a unique maximizer. We denote the unique maximizer by  $y^*$ .

From Proposition 1,  $\beta^* \equiv \beta_H(-\alpha) = \beta_L(-\alpha)$ . Note that  $\lim_{\gamma \rightarrow \infty} \beta^* = G^{-1}(1 - \tau) \in (-\bar{b}, \bar{b})$ . We consider two cases.

1. Suppose  $\beta \in [-\bar{b}, \beta^*)$ . Since  $\beta^* < \beta_H(y)$  for all  $y$ , we have  $\beta < \beta_H(y)$  for all  $y$ . Based on (41),

$$-q^*(y) = \begin{cases} \beta_L(y) & \text{if } \beta < \beta_L(y) \\ \beta & \text{if } \beta_L(y) \leq \beta. \end{cases}$$

Recall  $\lim_{\gamma \rightarrow \infty} \beta_L(y) = G^{-1}(1 - \frac{\tau}{1 - \alpha - y})$ . By the definition of  $\beta_L(\cdot)$ ,

$$\beta < \beta_L(y) \Leftrightarrow y < y_L,$$

where

$$y_L \equiv 1 - \alpha - \frac{\tau}{1 - G(\beta)} + \frac{1}{\gamma} \frac{G(\beta)}{1 - G(\beta)} (\mathbb{E}[b] - \mathbb{E}[b|b < \beta]) H(-\beta). \quad (55)$$

Notice, for large  $\gamma$  (where  $\beta_L(\cdot)$  is monotone),  $y_L < 0 \Leftrightarrow \beta > \beta_L(0)$ . Therefore,

$$\frac{\partial \Pi(y)}{\partial y} = (\beta - \mathbb{E}[b]) H(q^*(y)) - (2\gamma + \eta)y + \begin{cases} MPV(y) & \text{if } -\alpha < y < y_L \\ 0 & \text{if } y \geq y_L, \end{cases}$$

where

$$MPV(y) = \frac{\partial \beta_L(y)}{\partial y} f(-\beta_L(y)) [\alpha(\beta - \beta_L(y)) + y(\beta - \mathbb{E}[b])].$$

Next, we argue  $\lim_{\gamma \rightarrow \infty} y^* = 0$ . Suppose not. Let  $\lim_{\gamma \rightarrow \infty} \beta_L(y^*) = \beta_L^{\text{lim}} = G^{-1}(1 - \frac{\tau}{1 - \alpha - \lim_{\gamma \rightarrow \infty} y^*})$ . Then,

$$\left| \lim_{\gamma \rightarrow \infty} MPV(y^*) \right| = \left| -\frac{1 - G(\beta_L^{\text{lim}})}{g(\beta_L^{\text{lim}})} \frac{f(-\beta_L^{\text{lim}})}{1 - \alpha - \lim_{\gamma \rightarrow \infty} y^*} \left[ \alpha(\beta - \beta_L^{\text{lim}}) + \lim_{\gamma \rightarrow \infty} y^* (\beta - \mathbb{E}[b]) \right] \right| < \infty. \quad (56)$$

Since  $\lim_{\gamma \rightarrow \infty} y^* \neq 0$ , it must be

$$\left| \lim_{\gamma \rightarrow \infty} \frac{\partial \Pi(y)}{\partial y} \Big|_{y=y^*} \right| = \left| \lim_{\gamma \rightarrow \infty} (2\gamma + \eta)y^* \right| = \infty.$$

If  $\lim_{\gamma \rightarrow \infty} y^* \neq \lim_{\gamma \rightarrow \infty} y_L$  then it contradicts  $\frac{\partial \Pi(y)}{\partial y} \Big|_{y=y^*} = 0$ . Suppose  $\lim_{\gamma \rightarrow \infty} y^* = \lim_{\gamma \rightarrow \infty} y_L$ . In this case,  $\frac{\partial \Pi(y)}{\partial y} \Big|_{y^* \nearrow y_L}$  and  $\frac{\partial \Pi(y)}{\partial y} \Big|_{y^* \searrow y_L}$  have the same sign, which contradicts the optimality of  $y^*$ . Therefore,  $\lim_{\gamma \rightarrow \infty} y^* = 0$ .

Since  $\lim_{\gamma \rightarrow \infty} y^* = 0$  and  $\lim_{\gamma \rightarrow \infty} y_L < 0 \Leftrightarrow \beta > \lim_{\gamma \rightarrow \infty} \beta_L(0)$ , the blockholder is the median voter in the limit if and only if  $\beta \geq \lim_{\gamma \rightarrow \infty} \beta_L(0)$ . Fix a large  $\gamma$ , and let  $\varepsilon > 0$  be arbitrarily small such that  $-\bar{b} < \beta_L(0) - \varepsilon$  and  $\beta_L(0) + \varepsilon < \beta^*$  (notice  $\lim_{\gamma \rightarrow \infty} \beta_L(0) < \lim_{\gamma \rightarrow \infty} \beta^* \Leftrightarrow G^{-1}(\frac{1 - \alpha - \tau}{1 - \alpha}) < G^{-1}(1 - \tau)$ ). There are three cases:

- (a) If  $\beta \in (\beta_L(0) + \varepsilon, \beta^*)$  then  $y^* \approx 0 > y_L$ . Hence,  $\beta_L(y^*) \leq \beta$ ,  $q^*(y^*) = -\beta$ ,  $MPV(y^*) = 0$ , and the maximizer of  $\Pi(y)$  is

$$y^{**} \equiv \frac{1}{2\gamma + \eta} (\beta - \mathbb{E}[b]) H(-\beta).$$

Since  $y^* = y^{**}$ , based on (16),

$$\begin{aligned} p^*(y^*) &= \gamma y^* + v(\mathbb{E}[b], q^*(y^*)) \\ &= \gamma y^{**} + v(\mathbb{E}[b], -\beta) \\ &= \frac{\gamma}{2\gamma + \eta} (\beta - \mathbb{E}[b]) H(-\beta) + v_0 + (\mathbb{E}[b] + \mathbb{E}[\theta|q > -\beta]) H(-\beta) \\ &= v_0 + \left( \frac{\gamma}{2\gamma + \eta} (\beta - \mathbb{E}[b]) + \mathbb{E}[b] + \mathbb{E}[\theta|q > -\beta] \right) H(-\beta) \\ &= v(b^*, -\beta), \end{aligned}$$

as required.

- (b) If  $\beta \in (-\bar{b}, \beta_L(0) - \varepsilon)$  then  $y^* \approx 0 < y_L$ . Hence,  $\beta_L(y^*) > \beta$ ,  $q^*(y^*) = -\beta_L(y^*)$ , and the maximizer of  $\Pi(y)$  is

$$y^* = \frac{1}{2\gamma + \eta} (\beta - \mathbb{E}[b]) H(-\beta_L(y^*)) + \frac{1}{2\gamma + \eta} MPV(y^*).$$

Based on (16),

$$\begin{aligned} p^*(y^*) &= \gamma y^* + v(\mathbb{E}[b], -\beta_L(y^*)) \\ &= \frac{\gamma}{2\gamma + \eta} (\beta - \mathbb{E}[b]) H(-\beta_L(y^*)) + \frac{\gamma}{2\gamma + \eta} MPV(y^*) + v(\mathbb{E}[b], -\beta_L(y^*)) \\ &= v(b^*, -\beta_L(y^*)) + \frac{\gamma}{2\gamma + \eta} MPV(y^*), \end{aligned}$$

as required. Notice  $\lim_{\gamma \rightarrow \infty} \beta_L(y^*) = \lim_{\gamma \rightarrow \infty} \beta_L(0) = G^{-1}(1 - \frac{\tau}{1-\alpha})$  and

$$\lim_{\gamma \rightarrow \infty} MPV(y^*) = -\frac{1 - G(\lim_{\gamma \rightarrow \infty} \beta_L(0))}{g(\lim_{\gamma \rightarrow \infty} \beta_L(0))} \frac{f(-\lim_{\gamma \rightarrow \infty} \beta_L(0))}{1 - \alpha} \alpha(\beta - \lim_{\gamma \rightarrow \infty} \beta_L(0)) > 0.$$

Indeed,  $\beta < \beta_L(0) - \varepsilon$  implies  $\beta < \lim_{\gamma \rightarrow \infty} \beta_L(0)$  and hence it must be  $MPV(y^*) > 0$  for large  $\gamma$ .

- (c) Suppose  $\beta \in (\beta_L(0) - \varepsilon, \beta_L(0) + \varepsilon)$ . Notice

$$\frac{\partial \Pi(y, \beta)}{\partial y} \Big|_{y=0} = \begin{cases} (\beta - \mathbb{E}[b]) H(-\beta_L(0)) - \frac{\partial \beta_L(y)}{\partial y} \Big|_{y=0} f(-\beta_L(0)) \alpha(\beta_L(0) - \beta) & \text{if } \beta < \beta_L(0) \\ (\beta - \mathbb{E}[b]) H(-\beta) & \text{if } \beta \geq \beta_L(0), \end{cases}$$

and

$$\lim_{\beta \rightarrow \beta_L(0)} \frac{\partial \Pi(y, \beta)}{\partial y} \Big|_{y=0} = (\beta_L(0) - \mathbb{E}[b]) H(-\beta_L(0)).$$

Therefore:

- i. If  $\beta_L(0) > \mathbb{E}[b]$  then  $\lim_{\beta \rightarrow \beta_L(0)} \frac{\partial \Pi(y, \beta)}{\partial y} \Big|_{y=0} > 0$ . From the concavity of  $\Pi$ , if  $\beta \in (\beta_L(0) - \varepsilon, \beta_L(0) + \varepsilon)$  then  $y^* > 0$ . Since  $\beta'_L < 0$ , it must be  $\beta_L(y^*) < \beta_L(0)$ . Therefore, there is  $\underline{\beta} \in (-\bar{b}, \beta_L(0))$  such that if  $\beta \in (\underline{\beta}, \beta^*)$  then  $\beta_L(y^*) \leq \beta$  and case 1.a applies, and if  $\beta \in (-\bar{b}, \underline{\beta})$  then  $\beta < \beta_L(y^*)$  and case 1.b applies.
  - ii. If  $\beta_L(0) < \mathbb{E}[b]$  then  $\lim_{\beta \rightarrow \beta_L(0)} \frac{\partial \Pi(y, \beta)}{\partial y} \Big|_{y=0} < 0$ . From the concavity of  $\Pi$ , if  $\beta \in (\beta_L(0) - \varepsilon, \beta_L(0) + \varepsilon)$  then  $y^* < 0$ . Since  $\beta'_L < 0$ , in those cases  $\beta_L(0) < \beta_L(y^*)$ . Therefore, there is  $\underline{\beta} \in (\beta_L(0), \beta^*)$  such that if  $\beta \in (\underline{\beta}, \beta^*)$  then  $\beta_L(y^*) \leq \beta$  and case 1.a applies, and if  $\beta \in (-\bar{b}, \underline{\beta})$  then  $\beta < \beta_L(y^*)$  and case 1.b applies.
2. Suppose  $\beta \in (\beta^*, \bar{b}]$ . Since  $\beta^* > \beta_L(y)$  for all  $y$ , we have  $\beta > \beta_L(y)$  for all  $y$ , and based on (41),

$$-q^*(y) = \begin{cases} \beta & \text{if } \beta \leq \beta_H(y) \\ \beta_H(y) & \text{if } \beta_H(y) < \beta \end{cases}$$

Recall  $\lim_{\gamma \rightarrow \infty} \beta_H(y) = G^{-1}(\frac{1-\tau}{1-\alpha-y})$ . By the definition of  $\beta_H(\cdot)$ ,

$$\beta > \beta_H(y) \Leftrightarrow y < y_H,$$

where

$$y_H = 1 - \alpha - \frac{1 - \tau}{G(\beta)} - \frac{1}{\gamma} (\mathbb{E}[b] - \mathbb{E}[b|b < \beta]) H(-\beta). \quad (57)$$

Notice, for large  $\gamma$  (where  $\beta_H(\cdot)$  is monotone),  $y_H < 0 \Leftrightarrow \beta < \beta_H(0)$ . Therefore,

$$\frac{\partial \Pi(y)}{\partial y} = (\beta - \mathbb{E}[b]) H(q^*(y)) - (2\gamma + \eta)y + \begin{cases} MPV(y) & \text{if } -\alpha < y < y_H \\ 0 & \text{if } y \geq y_H, \end{cases}$$

where

$$MPV(y) = \frac{\partial \beta_H(y)}{\partial y} f(-\beta_H(y)) [\alpha(\beta - \beta_H(y)) + y(\beta - \mathbb{E}[b])].$$

Next, we argue  $\lim_{\gamma \rightarrow \infty} y^* = 0$ . Suppose not. Let  $\lim_{\gamma \rightarrow \infty} \beta_H(y^*) = \beta_H^* \lim = G^{-1}(\frac{1-\tau}{1-\alpha-\lim_{\gamma \rightarrow \infty} y^*})$ . Then,

$$\left| \lim_{\gamma \rightarrow \infty} MPV(y^*) \right| = \left| \frac{G(\beta_H^* \lim)}{g(\beta_H^* \lim)} \frac{f(-\beta_H^* \lim)}{1 - \alpha - \lim_{\gamma \rightarrow \infty} y^*} \left[ \alpha(\beta - \beta_H^* \lim) + \lim_{\gamma \rightarrow \infty} y^* (\beta - \mathbb{E}[b]) \right] \right| < \infty. \quad (58)$$

Since  $\lim_{\gamma \rightarrow \infty} y^* \neq 0$ , it must be

$$\left| \lim_{\gamma \rightarrow \infty} \frac{\partial \Pi(y)}{\partial y} \Big|_{y=y^*} \right| = \left| \lim_{\gamma \rightarrow \infty} (2\gamma + \eta)y^* \right| = \infty.$$

If  $\lim_{\gamma \rightarrow \infty} y^* \neq \lim_{\gamma \rightarrow \infty} y_H$  then it contradicts  $\frac{\partial \Pi(y)}{\partial y} \Big|_{y=y^*} = 0$ . Suppose  $\lim_{\gamma \rightarrow \infty} y^* = \lim_{\gamma \rightarrow \infty} y_H$ . In this case,  $\frac{\partial \Pi(y)}{\partial y} \Big|_{y^* \nearrow y_H}$  and  $\frac{\partial \Pi(y)}{\partial y} \Big|_{y^* \searrow y_H}$  have the same sign, which contra-

dicts the optimality of  $y^*$ . Therefore,  $\lim_{\gamma \rightarrow \infty} y^* = 0$ .

Since  $\lim_{\gamma \rightarrow \infty} y^* = 0$  and  $\lim_{\gamma \rightarrow \infty} y_H < 0 \Leftrightarrow \beta > \lim_{\gamma \rightarrow \infty} \beta_H(0)$ , the blockholder is the median voter in the limit if and only if  $\beta \leq \lim_{\gamma \rightarrow \infty} \beta_H(0)$ . Fix a large  $\gamma$ , and let  $\varepsilon > 0$  be arbitrarily small such that  $\beta^* < \beta_H(0) - \varepsilon$  and  $\beta_H(0) + \varepsilon < \bar{b}$  (notice  $\lim_{\gamma \rightarrow \infty} \beta_H(0) > \lim_{\gamma \rightarrow \infty} \beta^* \Leftrightarrow G^{-1}(\frac{1-\tau}{1-\alpha}) > G^{-1}(1-\tau)$ ). There are three cases:

- (a) If  $\beta \in (\beta^*, \beta_H(0) - \varepsilon)$  then  $y^* \approx 0 > y_H$ . Hence,  $\beta \leq \beta_H(y^*)$  and  $q^*(y) = -\beta$ . Similar to part 1.a,  $y^* = y^{**}$ ,  $MPV(y^*) = 0$ , and  $p^*(y^*) = v(b^*, -\beta)$ , as required.
- (b) If  $\beta \in (\beta_H(0) + \varepsilon, \bar{b})$  then  $y^* \approx 0 < y_H$ . Hence,  $\beta > \beta_H(y^*)$ ,  $q^*(y^*) = -\beta_H(y^*)$  and the maximizer of  $\Pi(y)$  is

$$y^* = \frac{1}{2\gamma + \eta} (\beta - \mathbb{E}[b]) H(-\beta_H(y^*)) + \frac{1}{2\gamma + \eta} MPV(y^*). \quad (59)$$

Based on (16), and similar to part 1.b,

$$p^*(y^*) = v(b^*, -\beta_H(y^*)) + \frac{\gamma}{2\gamma + \eta} MPV(y^*),$$

as required. Notice  $\lim_{\gamma \rightarrow \infty} \beta_H(y^*) = \lim_{\gamma \rightarrow \infty} \beta_H(0) = G^{-1}(\frac{1-\tau}{1-\alpha})$  and

$$\lim_{\gamma \rightarrow \infty} MPV(y^*(\gamma)) = \frac{G(\lim_{\gamma \rightarrow \infty} \beta_H(0)) f(-\lim_{\gamma \rightarrow \infty} \beta_H(0))}{g(\lim_{\gamma \rightarrow \infty} \beta_H(0))} \frac{1}{1-\alpha} \alpha(\beta - \lim_{\gamma \rightarrow \infty} \beta_H(0)) > 0.$$

Indeed,  $\beta > \beta_H(0) + \varepsilon$  implies  $\beta > \lim_{\gamma \rightarrow \infty} \beta_H(0)$  and hence it must be  $MPV(y^*) > 0$  for large  $\gamma$ .

- (c) Suppose  $\beta \in (\beta_H(0) - \varepsilon, \beta_H(0) + \varepsilon)$ . Notice

$$\frac{\partial \Pi(y, \beta)}{\partial y} \Big|_{y=0} = \begin{cases} (\beta - \mathbb{E}[b]) H(-\beta_H(0)) - \frac{\partial \beta_H(y)}{\partial y} \Big|_{y=0} f(-\beta_H(0)) \alpha(\beta_H(0) - \beta) & \text{if } \beta > \beta_H(0) \\ (\beta - \mathbb{E}[b]) H(-\beta) & \text{if } \beta \leq \beta_H(0) \end{cases}$$

and

$$\lim_{\beta \rightarrow \beta_H(0)} \frac{\partial \Pi(y, \beta)}{\partial y} \Big|_{y=0} = (\beta_H(0) - \mathbb{E}[b]) H(-\beta_H(0)).$$

Therefore:

- i. If  $\beta_H(0) > \mathbb{E}[b]$  then  $\lim_{\beta \rightarrow \beta_H(0)} \frac{\partial \Pi(y, \beta)}{\partial y} \Big|_{y=0} > 0$ . From the concavity of  $\Pi$ , if  $\beta \in (\beta_H(0) - \varepsilon, \beta_H(0) + \varepsilon)$  then  $y^* > 0$ . Since  $\beta'_H > 0$ , in those cases  $\beta_H(0) < \beta_H(y^*)$ . Therefore, there is  $\bar{\beta} \in (\beta_H(0), \bar{b})$  such that if  $\beta \in (\beta^*, \bar{\beta})$  then  $\beta \leq \beta_H(y^*)$  and case 2.a applies, and if  $\beta \in (\bar{\beta}, \bar{b})$  then  $\beta > \beta_H(y^*)$  and case 2.b applies.
- ii. If  $\beta_H(0) < \mathbb{E}[b]$  then  $\lim_{\beta \rightarrow \beta_H(0)} \frac{\partial \Pi(y, \beta)}{\partial y} \Big|_{y=0} < 0$ . From the concavity of  $\Pi$ , if  $\beta \in (\beta_H(0) - \varepsilon, \beta_H(0) + \varepsilon)$  then  $y^* < 0$ . Since  $\beta'_H > 0$ , in those cases  $\beta_H(y^*) < \beta_H(0)$ . Therefore, there is  $\bar{\beta} \in (\beta^*, \beta_H(0))$  such that if  $\beta \in (\beta^*, \bar{\beta})$  then  $\beta \leq \beta_H(y^*)$  and case 2.a applies, and if  $\beta \in (\bar{\beta}, \bar{b})$  then  $\beta > \beta_H(y^*)$  and case 2.b applies.



■

**Proof of Proposition 3.** The cutoffs  $\underline{\beta}$  and  $\bar{\beta}$  in the statement of the proposition follows from the proof of Proposition 2. Notice,  $\underline{\beta} < \beta^* < \bar{\beta}$ . Based on parts 1.a and 2.a of that proof, if  $\beta \in (\underline{\beta}, \beta^*)$  or  $\beta \in (\beta^*, \bar{\beta})$  then  $-q^*(y^*) = \beta$ ,  $MPV = 0$ , and hence the median voter is the blockholder and the voting premium is zero. Based on part 1.b (2.b) of that proof, if  $\beta \in (-\bar{b}, \underline{\beta})$  ( $\beta \in (\bar{\beta}, \bar{b})$ ) then  $-q^*(y^*) = \beta_L(y^*) > \beta$  ( $-q^*(y^*) = \beta_H(y^*) < \beta$ ),  $MPV > 0$ , and hence the median voter is a dispersed shareholder with a smaller (larger) bias toward the proposal than the blockholder, and the voting premium is strictly positive. Finally, if  $\beta > \bar{\beta}$  ( $\beta < \underline{\beta}$ ), that the voting premium is strictly positive and increases (decreases) in  $\beta$  follows from Lemma 4 in the Online Appendix.

By definition,  $\beta_L(0)$  solves  $(1 - \alpha)(1 - R(\beta_L; 0, -\beta_L)) = \tau$  and  $\beta_H(0)$  solves  $(1 - \alpha)(1 - R(\beta_H; 0, -\beta_H)) = \tau - \alpha$  when  $\gamma$  is large. Therefore, for large  $\gamma$ ,  $\beta_L(0) < \beta_H(0)$ . Based on proof of Proposition 2, the following holds:

1. If  $\mathbb{E}[b] < \beta_L(0)$  then  $\underline{\beta} \in (-\bar{b}, \beta_L(0))$  and  $\bar{\beta} \in (\beta_H(0), \bar{b})$ . The following interesting cases emerge: If  $\underline{\beta} < \beta < \beta_L(0)$  or  $\beta_H(0) < \beta < \bar{\beta}$  then without trade (i.e., if  $y = 0$ ) then the median voter would be a dispersed shareholder. But under the optimal trade ( $y^* > 0$ ) the blockholder becomes the median voter. Intuitively, in those cases, the blockholder cash-flow motive of trade is sufficiently strong, and he has incentives to buy shares from dispersed shareholders who dislike the proposal (low  $\mathbb{E}[b]$ ).
2. If  $\mathbb{E}[b] \in (\beta_L(0), \beta_H(0))$  then  $\underline{\beta} \in (\beta_L(0), \beta^*)$  and  $\bar{\beta} \in (\beta_H(0), \bar{b})$ .
3. If  $\mathbb{E}[b] > \beta_H(0)$  then  $\underline{\beta} \in (\beta_L(0), \beta^*)$  and  $\bar{\beta} \in (\beta^*, \beta_H(0))$ . The following interesting cases emerge: If  $\beta_L(0) < \beta < \underline{\beta}$  or  $\bar{\beta} < \beta < \beta_H(0)$  then without trade (i.e., if  $y = 0$ ) then the median voter would be the blockholder. But under the optimal trade ( $y^* < 0$ ) the median voter is a dispersed shareholder. Intuitively, in those cases, the blockholder cash-flow motive of trade is sufficiently strong, and he has incentives to sell shares to dispersed shareholders who like the proposal (high  $\mathbb{E}[b]$ ).

■

**Proof of Proposition 4.** Notice that

$$\begin{aligned}
u(b) &= (e + x^*(b))v(b, q^*) - x^*(b)p^* - \frac{\gamma}{2}x^*(b)^2 \\
&= ev(b, q^*) + x^*(b)[v(b, q^*) - p^*] - \frac{\gamma}{2}x^*(b)^2 \\
&= ev(b, q^*) + \frac{v(b, q^*) - p^*}{\gamma}[v(b, q^*) - p^*] - \frac{\gamma}{2}\left[\frac{v(b, q^*) - p^*}{\gamma}\right]^2 \\
&= ev(b, q^*) + \frac{1}{2\gamma}[v(b, q^*) - p^*]^2 \\
&= ev(b, q^*) + \frac{1}{2\gamma}[v(b, q^*) - \gamma y^* - v(\mathbb{E}[b], q^*)]^2 \\
&= ev(b, q^*) + \frac{1}{2\gamma}[(b - \mathbb{E}[b])H(q^*) - \gamma y^*]^2 \\
&= ev(b, q^*) + \frac{(b - \mathbb{E}[b])^2 H(q^*)^2 - 2(b - \mathbb{E}[b])H(q^*)\gamma y^* + (\gamma y^*)^2}{2\gamma}
\end{aligned}$$

and

$$\begin{aligned}
W^* &= \int_{-\bar{b}}^{\bar{b}} u(b)g(b)db \\
&= e \int_{-\bar{b}}^{\bar{b}} v(b, q^*)g(b)db + \int_{-\bar{b}}^{\bar{b}} \left[ \frac{(b - \mathbb{E}[b])^2 H(q^*)^2 - 2(b - \mathbb{E}[b])H(q^*)\gamma y^* + (\gamma y^*)^2}{2\gamma} \right] g(b)db \\
&= ev(\mathbb{E}[b], q^*) + \frac{H(q^*)^2}{2\gamma} \int_{-\bar{b}}^{\bar{b}} (b - \mathbb{E}[b])^2 g(b)db + \frac{\gamma}{2}(y^*)^2 \\
&= ev(\mathbb{E}[b], q^*) + \frac{\sigma_b^2}{2\gamma} H(q^*)^2 + \frac{\gamma}{2}(y^*)^2
\end{aligned}$$

Thus,

$$\begin{aligned}
\frac{\partial W^*}{\partial \beta} &= e \frac{\partial v(\mathbb{E}[b], q^*)}{\partial q^*} \frac{\partial q^*}{\partial \beta} - \frac{\sigma_b^2}{\gamma} H(q^*) f(q^*) \frac{\partial q^*}{\partial \beta} + \gamma y^* \frac{\partial y^*}{\partial \beta} \\
&= -e(\mathbb{E}[b] + q^*) f(q^*) \frac{\partial q^*}{\partial \beta} - \frac{\sigma_b^2}{\gamma} H(q^*) f(q^*) \frac{\partial q^*}{\partial \beta} + \gamma y^* \frac{\partial y^*}{\partial \beta} \\
&= \left[ e(\mathbb{E}[b] + q^*) + \frac{\sigma_b^2}{\gamma} H(q^*) \right] f(q^*) \frac{\partial(-q^*)}{\partial \beta} + \gamma y^* \frac{\partial y^*}{\partial \beta}.
\end{aligned}$$

We consider two cases:

1. Suppose  $\beta > \bar{\beta}$ . Based on the proof of Lemma 4 and Proposition 3, for large  $\gamma$  we have  $-q^*(y^*) = \beta_H(y^*)$ ,  $MPV(y^*) > 0$ , and  $y^* = \frac{1}{2\gamma+\eta}(\beta - \mathbb{E}[b])H(-\beta_H(y^*)) +$

$\frac{1}{2\gamma+\eta}MPV(y^*)$ . Moreover,  $\frac{\partial(-q^*(y^*))}{\partial\beta} > 0$ ,  $\frac{\partial MPV(y^*)}{\partial\beta} > 0$ , and  $\frac{\partial y^*}{\partial\beta} > 0$ . Thus,

$$\frac{\partial W^*}{\partial\beta} = \left[ e(\mathbb{E}[b] - \beta_H(y^*)) + \frac{\sigma_b^2}{\gamma}H(-\beta_H(y^*)) \right] f(-\beta_H(y^*)) \frac{\partial\beta_H(y^*)}{\partial\beta} + \gamma y^* \frac{\partial y^*}{\partial\beta}.$$

Since  $\beta_H(y^*)$  does not depend on  $\beta$  directly, we can write  $\frac{\partial\beta_H(y^*)}{\partial\beta} = \frac{\partial\beta_H(y^*)}{\partial y} \frac{\partial y^*}{\partial\beta}$ . Notice  $\frac{\partial\beta_H(y^*)}{\partial\beta}, \frac{\partial y^*}{\partial\beta} > 0$  implies  $\frac{\partial\beta_H(y^*)}{\partial y} > 0$ . Thus,

$$\begin{aligned} \frac{\partial W^*}{\partial\beta} &= \left[ e(\mathbb{E}[b] - \beta_H(y^*)) + \frac{\sigma_b^2}{\gamma}H(-\beta_H(y^*)) \right] f(-\beta_H(y^*)) \frac{\partial\beta_H(y^*)}{\partial y} \frac{\partial y^*}{\partial\beta} + \gamma y^* \frac{\partial y^*}{\partial\beta} \\ &= \left( \left[ e(\mathbb{E}[b] - \beta_H(y^*)) + \frac{\sigma_b^2}{\gamma}H(-\beta_H(y^*)) \right] f(-\beta_H(y^*)) \frac{\partial\beta_H(y^*)}{\partial y} + \gamma y^* \right) \frac{\partial y^*}{\partial\beta}. \end{aligned}$$

Notice  $\lim_{\gamma \rightarrow \infty} \beta_H(y^*) = \lim_{\gamma \rightarrow \infty} \bar{\beta} = G^{-1}\left(\frac{1-\tau}{1-\alpha}\right)$ ,  $\lim_{\gamma \rightarrow \infty} \frac{\partial\beta_H(y^*)}{\partial y} \in (0, \infty)$ , and  $\lim_{\gamma \rightarrow \infty} \gamma y^* = \frac{1}{2}(\beta - \mathbb{E}[b])H(-G^{-1}\left(\frac{1-\tau}{1-\alpha}\right)) + \frac{1}{2}\lim_{\gamma \rightarrow \infty} MPV(y^*)$ . Thus,

$$\lim_{\gamma \rightarrow \infty} \frac{\partial W^*}{\partial\beta} = \left( \begin{array}{l} e(\mathbb{E}[b] - G^{-1}\left(\frac{1-\tau}{1-\alpha}\right)) f(-G^{-1}\left(\frac{1-\tau}{1-\alpha}\right)) \lim_{\gamma \rightarrow \infty} \frac{\partial\beta_H(y^*)}{\partial y} \\ + \frac{1}{2}(\beta - \mathbb{E}[b])H(-G^{-1}\left(\frac{1-\tau}{1-\alpha}\right)) + \frac{1}{2}\lim_{\gamma \rightarrow \infty} MPV(y^*) \end{array} \right) \times \lim_{\gamma \rightarrow \infty} \frac{\partial y^*}{\partial\beta}$$

Recall  $\beta > \bar{\beta}$  implies  $\lim_{\gamma \rightarrow \infty} MPV(y^*) > 0$ . Thus, if  $\beta > \mathbb{E}[b] \geq \bar{\beta}$  then  $\frac{\partial W^*}{\partial\beta} > 0$  for large  $\gamma$ . In this case, both  $\frac{\partial W^*}{\partial\beta} > 0$  and  $\frac{\partial MPV(y^*)}{\partial\beta} > 0$  as required.

From Lemma 2 and expression (58) in the proof of Proposition 2, we have

$$\begin{aligned} \lim_{\gamma \rightarrow \infty} MPV(y^*) &= \frac{1-\tau}{1-\alpha} \times \frac{f(-G^{-1}\left(\frac{1-\tau}{1-\alpha}\right))}{g(G^{-1}\left(\frac{1-\tau}{1-\alpha}\right))} \frac{\alpha}{1-\alpha} (\beta - G^{-1}\left(\frac{1-\tau}{1-\alpha}\right)) \\ &= \frac{1-\tau}{1-\alpha} \times \frac{f(-\lim_{\gamma \rightarrow \infty} \bar{\beta})}{g(\lim_{\gamma \rightarrow \infty} \bar{\beta})} \frac{\alpha}{1-\alpha} (\beta - \lim_{\gamma \rightarrow \infty} \bar{\beta}) \\ \lim_{\gamma \rightarrow \infty} \frac{\partial\beta_H(y^*)}{\partial y} &= \frac{G(G^{-1}\left(\frac{1-\tau}{1-\alpha}\right))}{g(G^{-1}\left(\frac{1-\tau}{1-\alpha}\right))(1-\alpha)} \\ &= \frac{G(\lim_{\gamma \rightarrow \infty} \bar{\beta})}{g(\lim_{\gamma \rightarrow \infty} \bar{\beta})(1-\alpha)} \end{aligned}$$

Therefore

$$\lim_{\gamma \rightarrow \infty} \frac{\partial W^*}{\partial\beta} = \left( \begin{array}{l} (\mathbb{E}[b] - \lim_{\gamma \rightarrow \infty} \bar{\beta}) \frac{1-\tau}{1-\alpha} \frac{f(-\lim_{\gamma \rightarrow \infty} \bar{\beta})}{g(\lim_{\gamma \rightarrow \infty} \bar{\beta})} + \frac{1}{2} \frac{1-\tau}{1-\alpha} \frac{f(-\lim_{\gamma \rightarrow \infty} \bar{\beta})}{g(\lim_{\gamma \rightarrow \infty} \bar{\beta})} \frac{\alpha}{1-\alpha} (\beta - \bar{\beta}) \\ + \frac{1}{2} (\beta - \mathbb{E}[b])H(-\lim_{\gamma \rightarrow \infty} \bar{\beta}) \end{array} \right) \times \lim_{\gamma \rightarrow \infty} \frac{\partial y^*}{\partial\beta}$$

- Suppose  $\beta < \bar{\beta}$ . Based on the proof of Lemma 4, for large  $\gamma$  we have  $-q^*(y^*) = \beta_L(y^*)$ ,  $MPV(y^*) > 0$ , and  $y^* = \frac{1}{2\gamma+\eta}(\beta - \mathbb{E}[b])H(-\beta_L(y^*)) + \frac{1}{2\gamma+\eta}MPV(y^*)$ . Moreover,  $\frac{\partial MPV(y^*)}{\partial\beta} < 0$ , and there is  $\underline{\alpha} > 0$  such that if  $\alpha > \underline{\alpha}$ , then  $\frac{\partial y^*}{\partial\beta} < 0$  and  $\frac{\partial\beta_L(y^*)}{\partial y} < 0$ .

Notice at  $\lim_{\gamma \rightarrow \infty} \beta_L(y^*) = \lim_{\gamma \rightarrow \infty} \underline{\beta} = G^{-1}(\frac{1-\alpha-\tau}{1-\alpha})$ ,  $\lim_{\gamma \rightarrow \infty} \frac{\partial \beta_L(y^*)}{\partial y} \in (-\infty, 0)$ , and  $\lim_{\gamma \rightarrow \infty} \gamma y^* = \frac{1}{2}(\beta - \mathbb{E}[b]) H(-G^{-1}(\frac{1-\alpha-\tau}{1-\alpha})) + \frac{1}{2} \lim_{\gamma \rightarrow \infty} MPV(y^*)$ . Thus, we can write

$$\lim_{\gamma \rightarrow \infty} \frac{\partial W^*}{\partial \beta} = \left( e(\mathbb{E}[b] - G^{-1}(\frac{1-\alpha-\tau}{1-\alpha})) f(-G^{-1}(\frac{1-\alpha-\tau}{1-\alpha})) \lim_{\gamma \rightarrow \infty} \frac{\partial \beta_L(y^*)}{\partial y} + \frac{1}{2}(\beta - \mathbb{E}[b]) H(-G^{-1}(\frac{1-\alpha-\tau}{1-\alpha})) + \frac{1}{2} \lim_{\gamma \rightarrow \infty} MPV(y^*) \right) \times \lim_{\gamma \rightarrow \infty} \frac{\partial y^*}{\partial \beta}$$

Notice  $\frac{\partial W^*}{\partial \beta} < 0$  if  $\beta - \mathbb{E}[b] > 0$  and  $\mathbb{E}[b] - G^{-1}(\frac{1-\alpha-\tau}{1-\alpha}) < 0$ . Recall  $\beta < \underline{\beta}$  implies  $\lim_{\gamma \rightarrow \infty} MPV(y^*) > 0$ . Thus, if  $\mathbb{E}[b] \leq \beta < \underline{\beta}$  then  $\frac{\partial W^*}{\partial \beta} < 0$  for large  $\gamma$ . In this case, both  $\frac{\partial W^*}{\partial \beta} < 0$  and  $\frac{\partial MPV(y^*)}{\partial \beta} < 0$  as required.

From Lemma 2 and expression (56) in the proof of Proposition 2, we have

$$\begin{aligned} \lim_{\gamma \rightarrow \infty} MPV(y^*) &= \frac{\tau}{1-\alpha} \frac{f(-G^{-1}(\frac{1-\alpha-\tau}{1-\alpha}))}{g(G^{-1}(\frac{1-\alpha-\tau}{1-\alpha}))} \frac{\alpha}{1-\alpha} (G^{-1}(\frac{1-\alpha-\tau}{1-\alpha}) - \beta) \\ &= \frac{\tau}{1-\alpha} \frac{f(-\lim_{\gamma \rightarrow \infty} \underline{\beta})}{g(\lim_{\gamma \rightarrow \infty} \underline{\beta})} \frac{\alpha}{1-\alpha} (\lim_{\gamma \rightarrow \infty} \underline{\beta} - \beta) \\ \lim_{\gamma \rightarrow \infty} \frac{\partial \beta_L(y^*)}{\partial y} &= -\frac{1 - G(G^{-1}(\frac{1-\alpha-\tau}{1-\alpha}))}{g(G^{-1}(\frac{1-\alpha-\tau}{1-\alpha}))(1-\alpha)} \\ &= -\frac{1 - G(\lim_{\gamma \rightarrow \infty} \underline{\beta})}{g(\lim_{\gamma \rightarrow \infty} \underline{\beta})(1-\alpha)} \end{aligned}$$

Therefore,

$$\lim_{\gamma \rightarrow \infty} \frac{\partial W^*}{\partial \beta} = \left( -(\mathbb{E}[b] - \lim_{\gamma \rightarrow \infty} \underline{\beta}) \frac{f(-\lim_{\gamma \rightarrow \infty} \underline{\beta})}{g(\lim_{\gamma \rightarrow \infty} \underline{\beta})} \frac{\tau}{1-\alpha} + \frac{1}{2}(\beta - \mathbb{E}[b]) H(-\lim_{\gamma \rightarrow \infty} \underline{\beta}) + \frac{1}{2} \frac{\tau}{1-\alpha} \frac{f(-\lim_{\gamma \rightarrow \infty} \underline{\beta})}{g(\lim_{\gamma \rightarrow \infty} \underline{\beta})} \frac{\alpha}{1-\alpha} (\lim_{\gamma \rightarrow \infty} \underline{\beta} - \beta) \right) \times \lim_{\gamma \rightarrow \infty} \frac{\partial y^*}{\partial \beta}$$

Notice that if  $\alpha < \underline{\alpha}$  then  $\lim_{\gamma \rightarrow \infty} \frac{\partial y^*}{\partial \beta} > 0$ . Thus, if  $\alpha \approx 0$  and  $\mathbb{E}[b] < \beta < \underline{\beta}$  then the first term is positive, the second term is positive, and the third term is arbitrarily small. In this case,  $\frac{\partial W^*}{\partial \beta} > 0 > \frac{\partial MPV(y^*)}{\partial \beta}$ .

■

**Proof of Corollary 2.** If  $b = E[b]$  for all dispersed shareholders, then their trades are  $x = -y$  from equation (10). Then  $r(b; y, q_e^*) = g(b)$  and  $R(b'; y, q_e^*) = G(b')$  from (11) and (12). Dispersed shareholders vote in favor if and only if  $q \geq -b$  and  $q^* = -b$ , because the median voter is always a dispersed shareholder, independently of how the blockholder votes, as long as  $\alpha + y < \tau$ . Hence,  $\frac{\partial(-q^*)}{\partial y} = 0$ , so the voting premium is zero from (27). ■

Proposition 5 is a special case of the following result.

**Proposition 7.** *Suppose  $\alpha = 0$ . There exist  $\bar{\gamma} < \infty$  such that if  $\gamma > \bar{\gamma}$ , then the equilibrium exists and is unique. Moreover, in equilibrium,*

(i) If  $\mathbb{E}[b] < \beta$ , then  $y^*$ ,  $q^*(y^*)$ , and  $p^*$  have the same functional forms as in Proposition 2. Moreover,  $MPV(y^*) < 0$  if and only if  $\beta < \underline{\beta}$ , where  $\underline{\beta}$  is defined in Proposition 3.

(ii) If  $\beta \leq \mathbb{E}[b]$ , then  $y^* = 0$  (the no-short-selling constraint binds),

$$-q^* = \begin{cases} \beta_L(0) & \text{if } \beta \leq \beta_L(0) \\ \beta_H(0) & \text{if } \beta_H(0) < \beta \end{cases} \quad (60)$$

$MPV(y^*) = 0$ , and  $p^* = v(\mathbb{E}[b], q^*)$ .

**Proof.** We build on the proof of Proposition 2, and adjust to the special case with  $\alpha = 0$ . For the same reasons as in the proof of Proposition 2,  $\lim_{\gamma \rightarrow \infty} y^* = 0$ , whether or not the short-sales constraint binds. Also, based on (56) and (58), if  $\alpha = 0$  then  $\lim_{\gamma \rightarrow \infty} MPV(y^*) = 0$ . Moreover,  $\alpha = 0$  implies  $\beta_H(0) = \beta_L(0) = \beta^*$ . This has the following implications for the proof of Proposition 2: Case 1.a is eliminated and the analysis therein is only relevant in the context of case 1.c.I. Similarly, case 2.a is eliminated and the analysis therein is only relevant in the context of case 2.c.I. Moreover, for case 1.c the relevant range is  $\beta \in (\beta_L(0) - \varepsilon, \beta_L(0))$ , and for case 2.c the relevant range is  $\beta \in (\beta_H(0), \beta_H(0) + \varepsilon)$ . Consider two cases:

1. Suppose  $\mathbb{E}[b] < \beta$ . Then,  $\frac{\partial \Pi(y, \beta)}{\partial y}|_{y=0} > 0$ , and for large  $\gamma$  we have  $y^* > 0$ . Therefore, the short-sales constraint does not bind, and  $y^*$ ,  $q^*(y^*)$ , and  $p^*$  have the same functional forms as in Proposition 2. Notice cases 1.c.II and 2.c.II in the proof of Proposition 2 are eliminated. Thus,  $\underline{\beta} \in (-\bar{b}, \beta_L(0))$  and  $\bar{\beta} \in (\beta_H(0), \bar{b})$ . If  $\beta \in (\underline{\beta}, \bar{\beta})$  then  $MPV(y^*) = 0$ . If  $\beta < \underline{\beta}$  then

$$MPV(y^*) = \frac{\partial \beta_L(y)}{\partial y}|_{y=y^*} f(-\beta_L(y^*)) y^* (\beta - \mathbb{E}[b]).$$

Since  $\frac{\partial \beta_L(y)}{\partial y}|_{y=y^*} < 0$  and  $y^* > 0$ , we have  $MPV(y^*) < 0$ . If  $\beta > \bar{\beta}$  then

$$MPV(y^*) = \frac{\partial \beta_H(y)}{\partial y}|_{y=y^*} f(-\beta_H(y^*)) y^* (\beta - \mathbb{E}[b]).$$

Since  $\frac{\partial \beta_H(y)}{\partial y}|_{y=y^*} > 0$  and  $y^* > 0$ , we have  $MPV(y^*) > 0$ , as required.

2. Suppose  $\mathbb{E}[b] \geq \beta$ . Then,  $\frac{\partial \Pi(y, \beta)}{\partial y}|_{y=0} \leq 0$ , and for large  $\gamma$  the short-sales constraint binds and  $y^* = 0$ . If  $y = 0$  then based the proof of Proposition 1, expression (41), and the observation that  $\beta_L(0) = \beta_H(0)$ , the median voter has a bias

$$-q^* = \begin{cases} \beta_L(0) & \text{if } \beta \leq \beta_L(0) \\ \beta_H(0) & \text{if } \beta_H(0) < \beta. \end{cases}$$

Based on (9), if  $y^* = 0$  then the share price is

$$\begin{aligned} p^* &= v(\mathbb{E}[b], q^*) \\ &= v(b^*, q^*) + \frac{\gamma}{2\gamma + \eta} (\mathbb{E}[b] - \beta) H(q^*). \end{aligned}$$

Since  $\alpha = 0$  and  $y^* = 0$ , then  $MPV(y^*) = 0$ .

■

**Proof of Proposition 6.** The objective  $\Pi(y, \hat{y})$  of the blockholder with dual-class shares can be rewritten as:

$$\begin{aligned}
\max_{y, \hat{y}} \Pi(y, \hat{y}) &= (\alpha + y) v(\beta, q^*(y)) - yp^*(y) - \frac{\eta}{2} y^2 + (\hat{\alpha} + \hat{y}) v(\beta, q^*(y)) - \hat{y} \hat{p}^*(\hat{y}) - \frac{\eta}{2} \hat{y}^2 \\
&= \alpha v(\beta, q^*(y)) + y(\beta - \mathbb{E}[b]) \Pr[q > q^*(y)] - (\gamma + \eta/2) y^2 \\
&\quad + \hat{\alpha} v(\beta, q^*(y)) + \hat{y}(\beta - \mathbb{E}[b]) \Pr[q > q^*(y)] - (\gamma + \eta/2) \hat{y}^2 \\
&= (\alpha + \hat{\alpha}) v(\beta, q^*(y)) + (y + \hat{y})(\beta - \mathbb{E}[b]) \Pr[q > q^*(y)] - (\gamma + \eta/2)(y^2 + \hat{y}^2) \\
&= (\alpha + \hat{\alpha}) v_0 + (\alpha + \hat{\alpha}) \Pr[q > q^*(y)] \mathbb{E}[\theta | q > q^*(y)] \\
&\quad + ((\alpha + \hat{\alpha} + y + \hat{y})\beta - (y + \hat{y})\mathbb{E}[b]) \Pr[q > q^*(y)] - (\gamma + \eta/2)(y^2 + \hat{y}^2).
\end{aligned}$$

We rewrite the first-order condition with respect to  $y$ ,  $\frac{\partial \Pi(y, \hat{y})}{\partial y} = 0$ , as

$$\begin{aligned}
&\left[ \begin{array}{c} \underbrace{(\beta - \mathbb{E}[b]) H(q^*(y)) - (2\gamma + \eta)y}_{\text{marginal payoff from buying cash flow rights}} \\ + \underbrace{\frac{\partial(-q^*(y))}{\partial y} f(q^*(y)) [(\alpha + \hat{\alpha})(q^*(y) + \beta) + (y + \hat{y})(\beta - \mathbb{E}[b])]}_{\text{marginal payoff from buying voting rights } MPV(y, \hat{y})} \end{array} \right] = 0 \Leftrightarrow \\
&(\beta - \mathbb{E}[b]) \Pr H(q^*(y)) - (2\gamma + \eta)y + MPV(y, \hat{y}) = 0 \Leftrightarrow \\
&y^* = \frac{1}{2\gamma + \eta} (\beta - \mathbb{E}[b]) H(q^*(y)) + \frac{1}{2\gamma + \eta} MPV(y, \hat{y}).
\end{aligned}$$

We rewrite the first-order condition with respect to  $\hat{y}$ ,  $\frac{\partial \Pi(y, \hat{y})}{\partial \hat{y}} = 0$ , as

$$\begin{aligned}
&\underbrace{(\beta - \mathbb{E}[b]) H(q^*(y)) - (2\gamma + \eta)\hat{y}}_{\text{marginal payoff from buying cash flow rights in non-voting shares}} = 0 \Leftrightarrow \\
&\hat{y}^* = \frac{1}{2\gamma + \eta} (\beta - \mathbb{E}[b]) H(q^*(y)),
\end{aligned}$$

which implies (38). ■

## Appendix - Table 1

The following table lists 40 studies that measure the voting premium using five different methodologies.<sup>31</sup> Methods of measurement within a given methodology may differ slightly. The studies on dual-class tender offers by [Bradley \(1980\)](#) and [DeAngelo and DeAngelo \(1985\)](#) are classified as block trades because tender offers are bids for a block of shares, not for individual shares. [Christoffersen et al. \(2007\)](#) is listed as two separate studies.

Study		Sample			Voting premium		
Authors	Year of publication	Country	Period	Size	Dual-class premium	Block-trade premium	Voting yield
<b>Panel A: Dual-class shares</b>							
Lease et al.	1983	USA	1940-1978	26	5.44%		
Levy	1983	Israel	1974-1980	25	45.50%		
Horner	1988	Switzerland	1973-1983	45	22.40%		
Megginson	1990	UK	1955-1982	152	13.30%	32.10%	
Zingales	1994	Italy	1987-1990	96	81.50%		
Smith and Amoako-Adu	1995	Canada	1981-1986	62	10.40%	57.20%	
Zingales	1995	USA	1984-1990	94	10.47%	81.50%	
Rydqvist	1996	Sweden	1983-1990	65	12.00%		
Kunz and Angel	1996	Switzerland	1990-1991	29	18.00%		
Maynes	1996	Canada	1984	46	6.66%		
Muus	1998	France	1986-1996	25	51.35%		
Chung and Kim	1999	Korea	1992-1993	119	9.60%		
Hoffmann-Burchardi	1999	Germany	1988-1997	84	26.30%	21.70%	
Cox and Roden	2002	USA	1984-1999	98	7.70%		
Daske and Ehrhardt	2002	Germany	1956-1998	101	17.23%	20.60%	
Dittmann	2003	Germany	1960-2001	82	12.62%		
Neumann	2003	Denmark	1992-1999	34	12.31%		
Nenova	2003	cross-country	1997	661	13.85%		
Muravyev	2004	Russia	1997-2003	37	64.72%		
Ødegaard	2007	Norway	1988-2005	226	5.60%		
Caprio and Croci	2008	Italy	1974-2003	116	56.51%		
Bigelli and Croci	2013	Italy	1999-2008	74	20.35%		
Broussard and Vaihekoski	2019	Finland	1982-2018	50	27.20%		

<sup>31</sup>The studies are: [Aggarwal, Saffi, and Sturgess \(2015\)](#); [Albuquerque and Schroth \(2010\)](#); [Albuquerque and Schroth \(2015\)](#); [Barak and Lauterbach \(2011\)](#); [Barclay and Holderness \(1989\)](#); [Bergström and Rydqvist \(1992\)](#); [Bigelli and Croci \(2013\)](#); [Bradley \(1980\)](#); [Broussard and Vaihekoski \(2019\)](#); [Caprio and Croci \(2008\)](#); [Christoffersen et al. \(2007\)](#); [Chung and Kim \(1999\)](#); [Cox and Roden \(2002\)](#); [Daske and Ehrhardt \(2002\)](#); [DeAngelo and DeAngelo \(1985\)](#); [Dittmann \(2003\)](#); [Dyck and Zingales \(2004\)](#); [Fos and Holderness \(2020\)](#); [Franks and Mayer \(2001\)](#); [Gurun and Karakas \(2020\)](#); [Hoffman-Burchardi \(1999\)](#); [Horner \(1988\)](#); [Jang, Kim, and Mohseni \(2019\)](#); [Kalay, Karakas, and Pant \(2014\)](#); [Kind and Poltera \(2013\)](#); [Kind and Poltera \(2017\)](#); [Kunz and Angel \(1996\)](#); [Lease, McConnell, and Mikkelsen \(1983\)](#); [Levy \(1983\)](#); [Maynes \(1996\)](#); [Megginson \(1990\)](#); [Muravyev \(2004\)](#); [Muus \(1998\)](#); [Nenova \(2003\)](#); [Neumann \(2003\)](#); [Odegaard \(2007\)](#); [Rydqvist \(1996\)](#); [Smith and Amoako-Adu \(1995\)](#); [Zingales \(1994\)](#); [Zingales \(1995\)](#).